

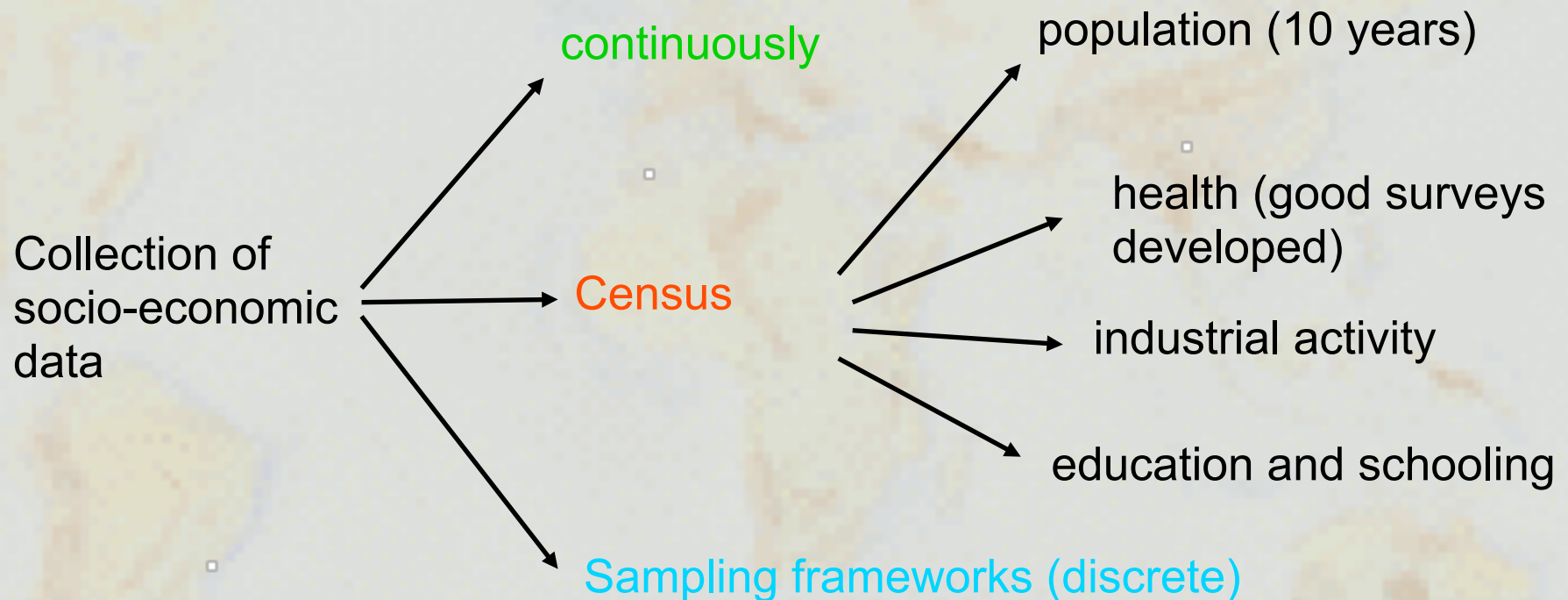
# L4:Thematic mapping



Kraak & Ormeling, Cartography – Visualization of Geospatial Data  
- chapter 7: Statistical mapping

# Statistical data collection

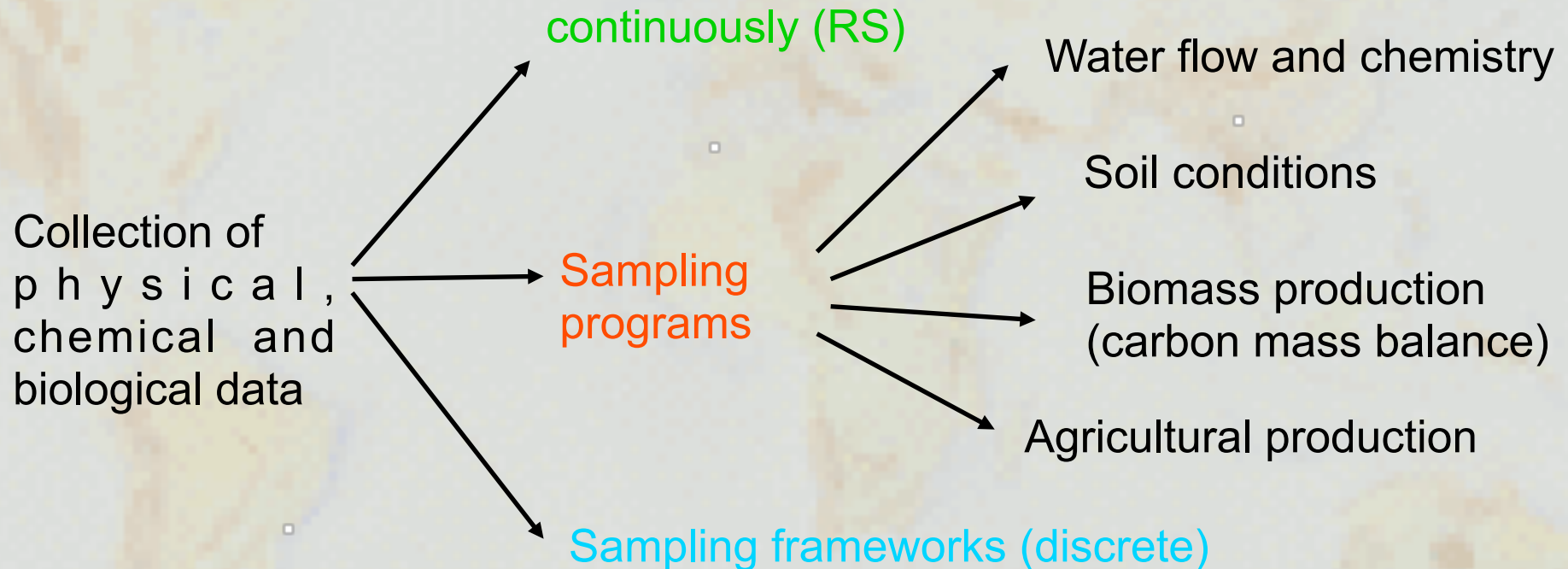
## Statistical surveys of socio-economic data



**Privacy regulations:** data are combined before publishing.  
Information on individual households, farms, plants, companies can not be worked out from the data.

# Statistical data collection

## Statistical surveys of physical, chemical and biological data



**Privacy regulations:** data are combined before publishing. Information on individual farms and plots can not be worked out from the data (dependent on legal regulations in country of study).

# Data analysis

After the collection of the data, these have to be analysed in order to choose the correct method for their representation and visualisation.

## 1. Assessing validity of the data:

- when were the data collected?
- in which way?
- for what purpose?
- for which period of time?
- to what area do they refer?
- are they comparable to older data (in order to realize a time series)?

Usefulness,  
reliability and  
accuracy of data

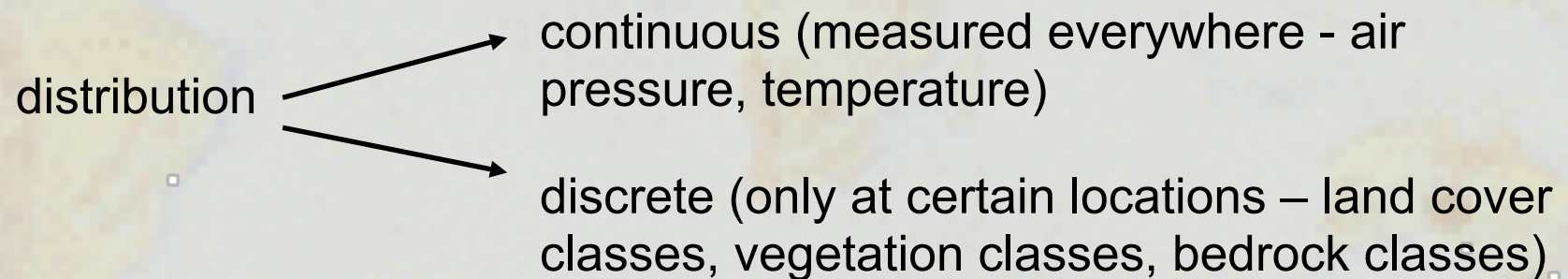
The description of the data is called metadata, and ideally the metadata should always follow the data, e.g. in the data-file header or as a separate file.

# Data analysis

## 2. Assessing data characteristics:

- the **nature of objects** the data refer to (point, linear, areal, volumetric objects)

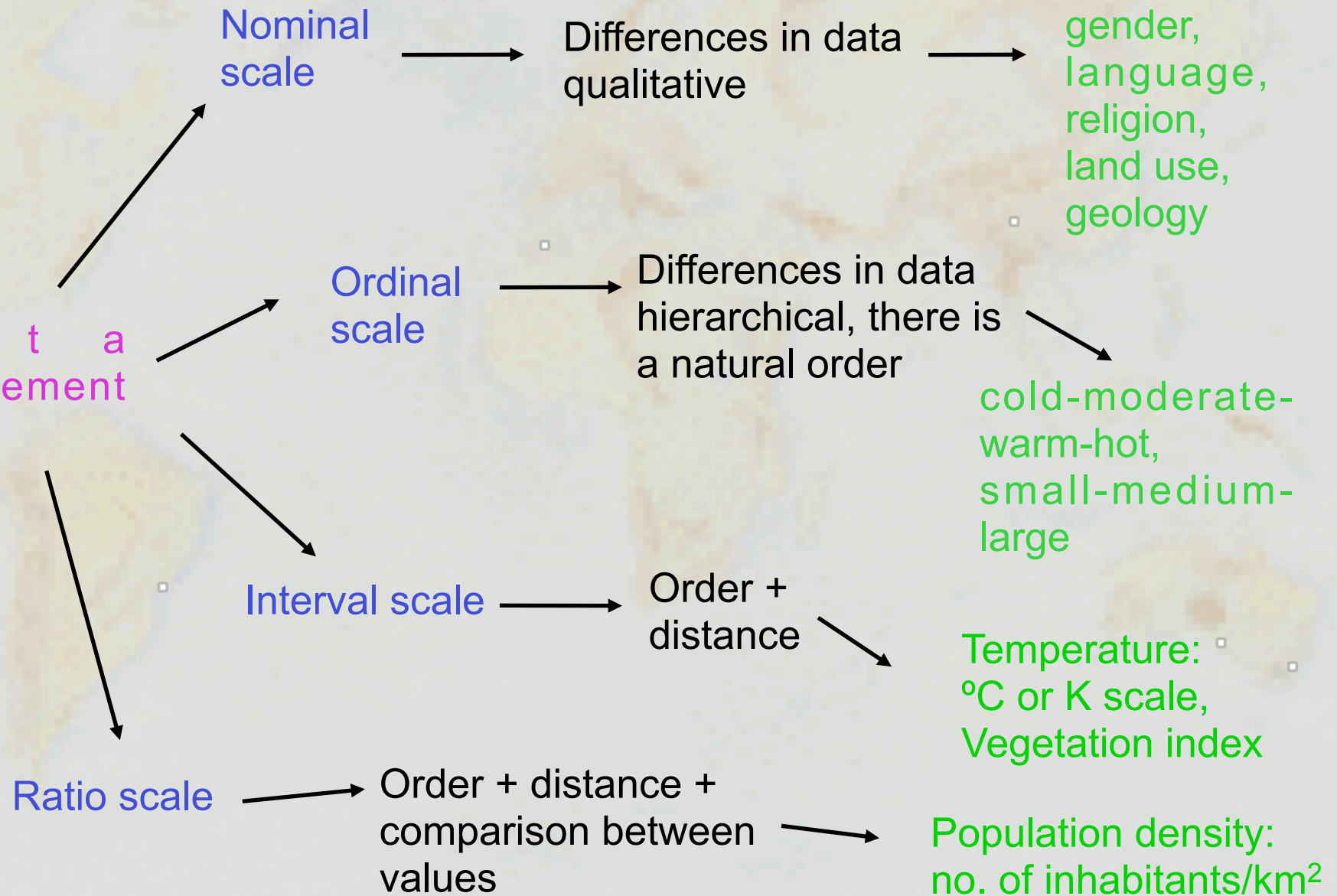
- the **type of change** in the data (gradual, abrupt), related to distribution



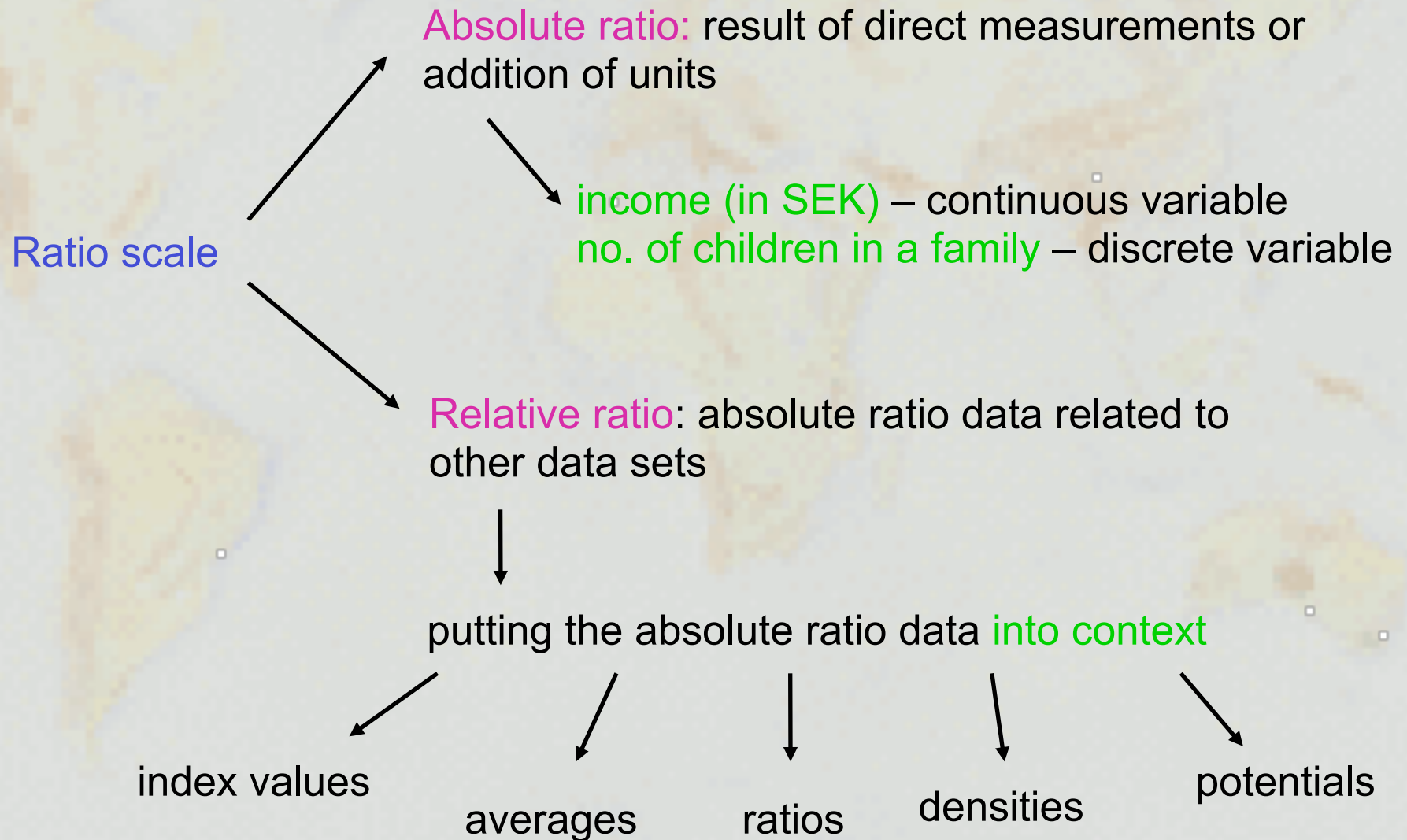
- the **measurement scale** (nominal, ordinal, interval, ratio)

# Data analysis

## Data measurement scales



# Data analysis



## Data analysis

**Index values** for time series:

- how much in today's money was 10000 SEK in 1950?

**Density:**

- ratio between the population of an area and the resources available to that population (either the residential area or the agricultural area they are cultivating)

**Non-area-related ratios:**

- relationship between any two data sets (no. of doctors/population),
- or relationship between two subsets of population (no. of doctors/no. of teachers)
- example:

total number of influenza patients in Sweden = 100000

total number of influenza patients in Italy = 120000

But, Sweden has ca. 9 million inhabitants and Italy ca. 60 million inhabitants!

A more objective comparison is to compare the ratios:

ratio of influenza patients/population =

ca. 1% (Sweden) = 0.2% (Italy)



# Data analysis

## Averages:

- characterisation of a data set by one number
- this is only successful for data with small variation in measurement
- **three different average measures:**

A series of given data values: 1, 1, 1, 1, 2, 3, 5, 10, 100

**mean** = sum of all values / number of all values =  
 $(1+1+1+1+2+3+5+10+100)/9 = 13.77$

**median** = the middle value (50% of all values are larger/smaller than this value) = 2

**mode** = the most frequent value = 1

## Data analysis

### Nearest neighbour index:

- distribution patterns of point locations, the topological characteristics of line patterns, the shape of areal patterns
- $R_n$  = comparison between random patterns and actual pattern:

$$R_n = \begin{cases} 0 \rightarrow \text{all observations in the actual pattern are in one point} \\ 1 \rightarrow \text{actual pattern is a totally random one} \\ 2.15 \rightarrow \text{actual pattern is completely regular (distances} \\ \quad \text{between all points equal)} \end{cases}$$

*Table 1* Nearest neighbour index values of places over 10 000 inhabitants per province in the Netherlands

Drenthe	1.6
Overijssel	1.5
Limburg	1.20
Friesland	1.18
Noord-Holland	1.16
Noord-Brabant	1.15
Gelderland	1.08
Zeeland	1.04
Zuid-Holland	1.01
Utrecht	1.0
Groningen	0.93
Flevoland	2.1



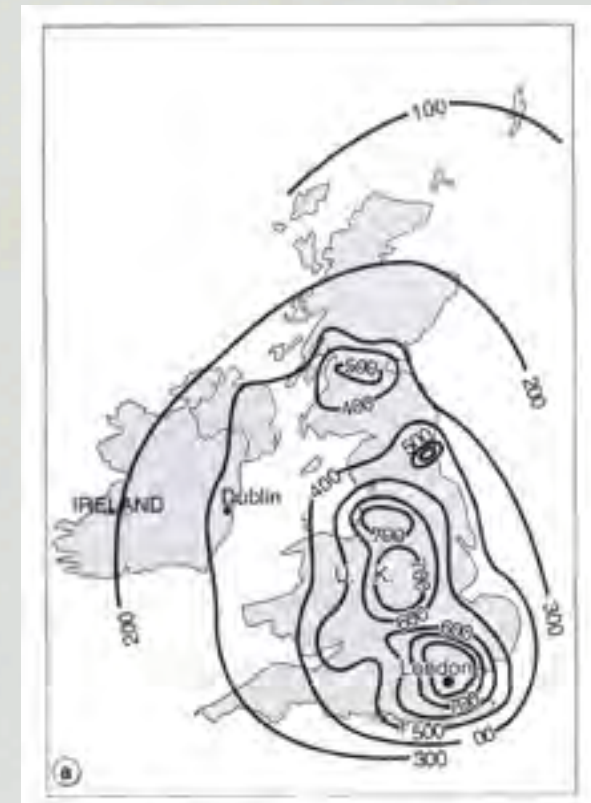
Figure 7.4 Population centres with over 10 000 inhabitants in the Netherlands

## Data analysis

### Potentials:

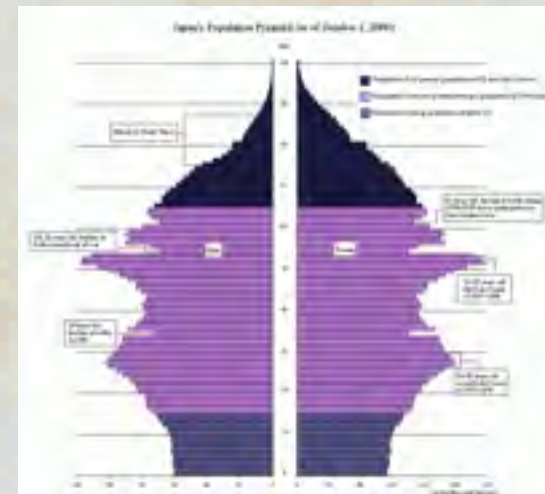
- potential in physics = attraction between two masses =  $(m_1 * m_2) / d(m_1, m_2)$
- in geography:
  - virtual interaction between
  - the inhabitants of different cities = population potential
  - expected purchases in a market = market potential
- **population potential** at a certain location = chance that the people at that location would meet people from other locations (neighbour cities)

Interval scale of human interactions in the UK and Ireland



## Data adjustment

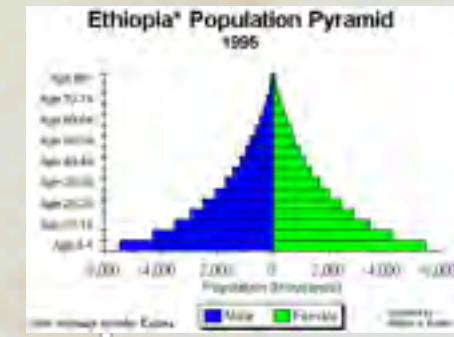
**Normalisation** – to minimize the distorting effects of irregularities in the population structure or geographical features



## Data adjustment

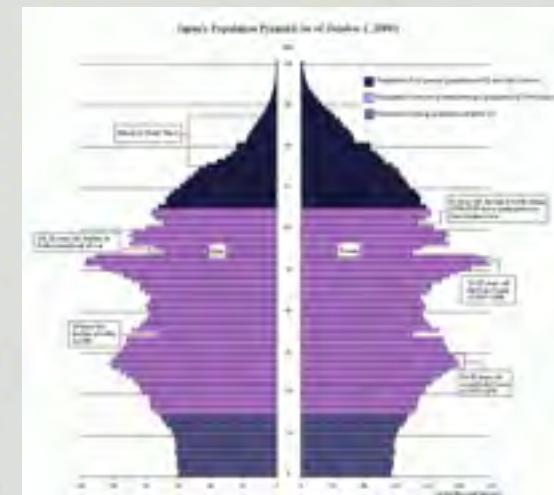
### Example 1:

- **birth rate** = number of births / 1000 inhabitants
- **death rate** = number of deaths / 1000 inhabitants



But birth and death rate depends on the form of the population pyramide.

In an area with a large amount of old people, death rate will be higher and birth rate lower than in an area with a normal population.



Data adjustment **necessary!**

- **fertility rate** = number of births / 1000 women in child-bearing age

## Data adjustment

### Example 2:

physical geography - minimizing effects of relief upon climate

0.6°C degree decrease in temperature for each 100m of elevation



All temperatures can be adjusted to their sea-level values.

## Data classification

Mapping unprocessed data → Unclear visualisation



**Data classification**: systematical grouping of data based on one or more characteristics

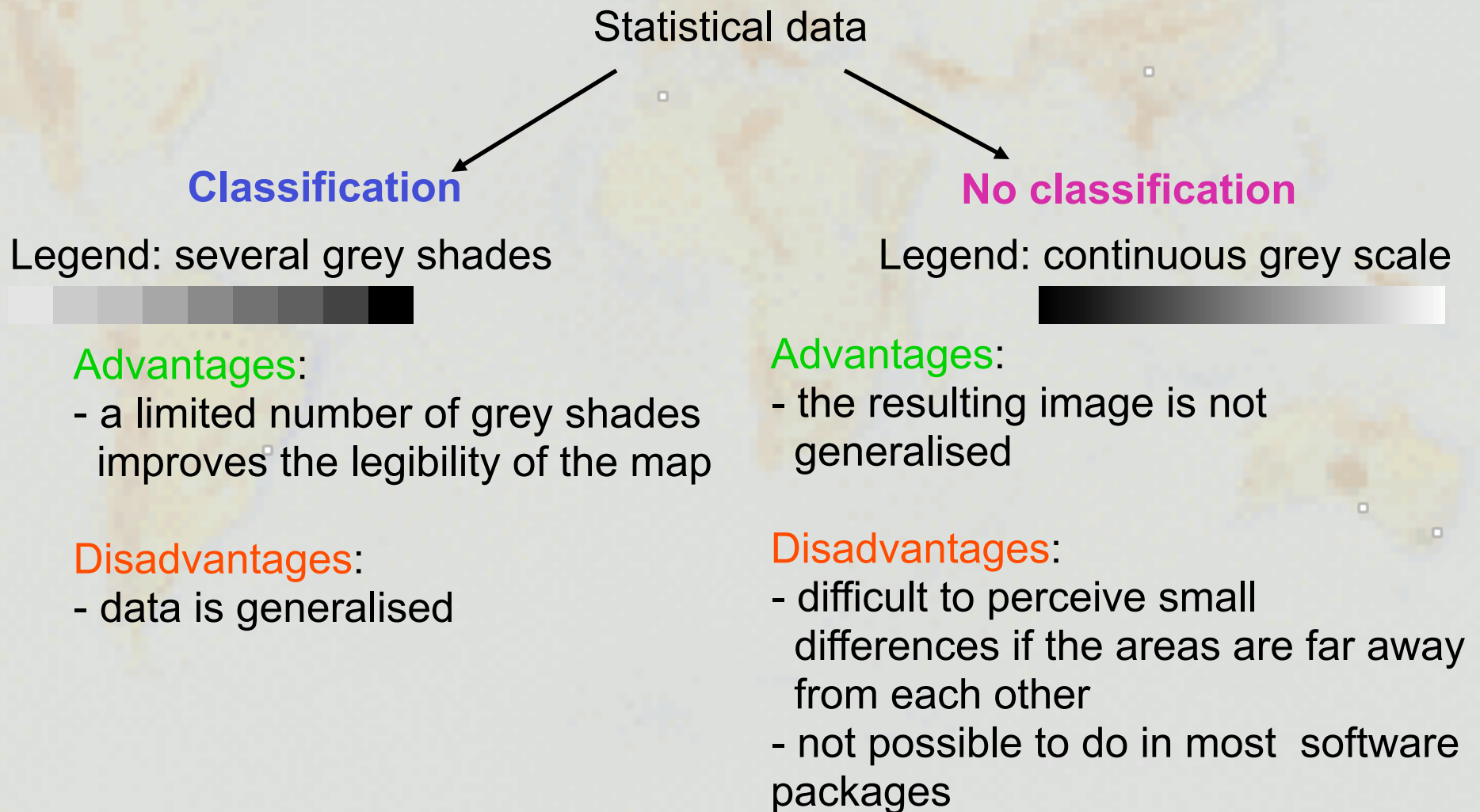


Clearer map image

The data classification can be done either by producing a new thematic layer, or by symbolisation of the original data into discrete classes.

## Data classification

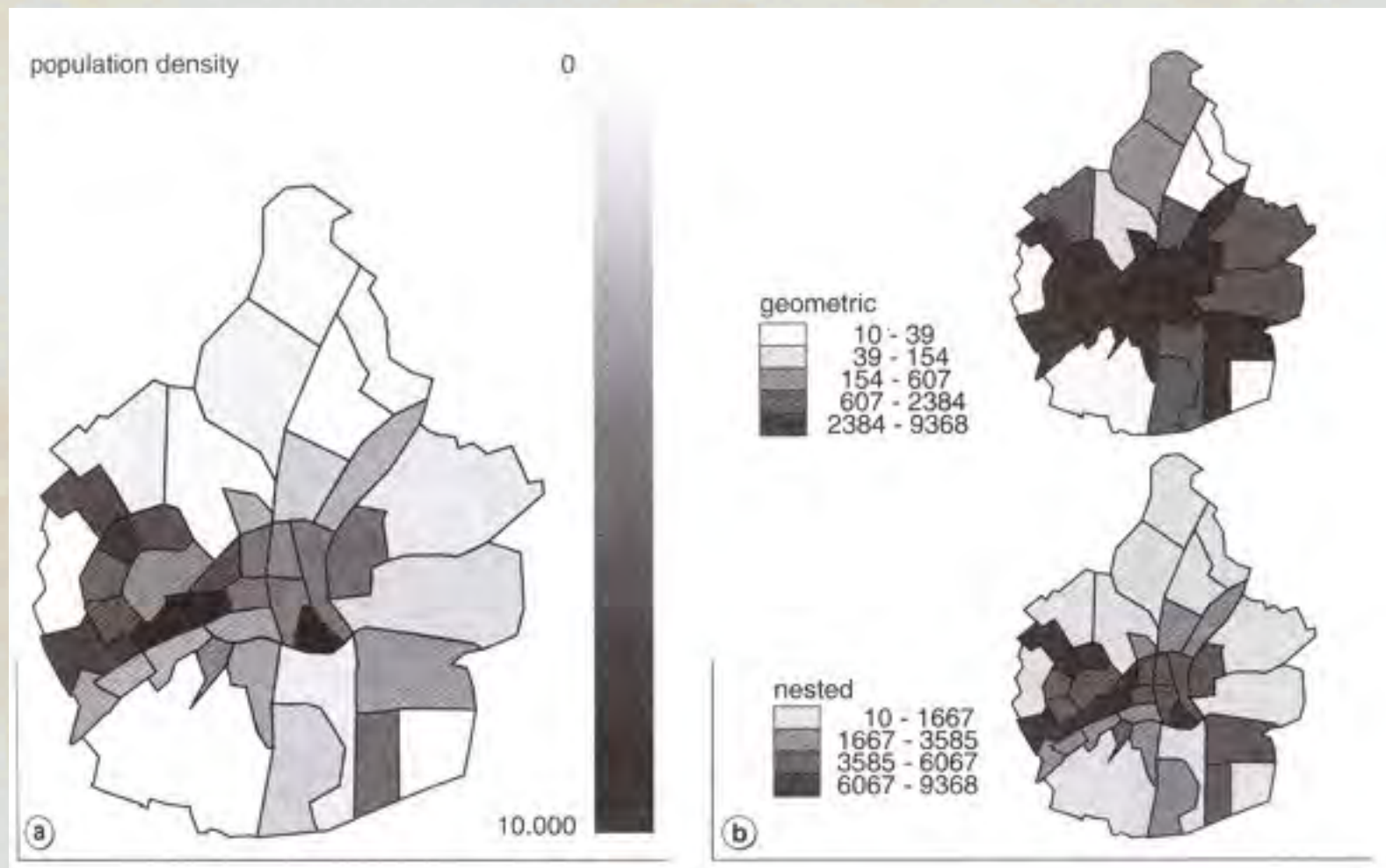
Limit the number of classes: humans can handle **approx. 7 classes** to get an overview and understanding the mapped theme at a glance.





## Data classification

### Classification vs. no classification



## Data classification

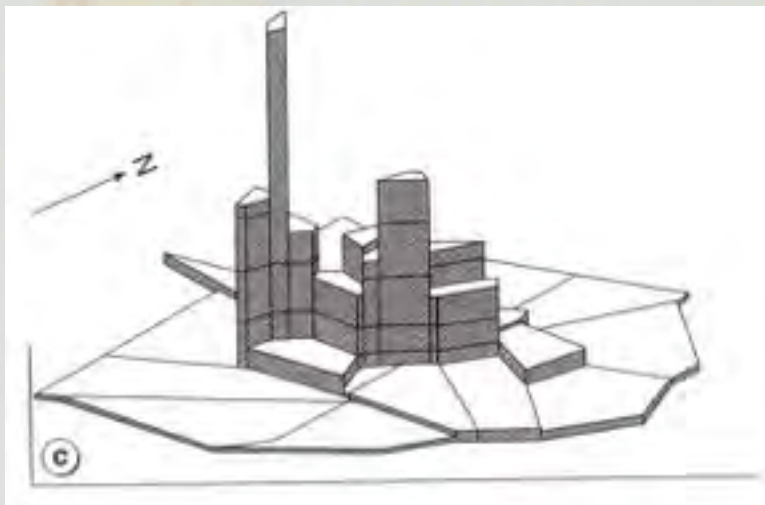
### Classification requirements:

1. The final map has to be as close to the actual statistical surface as possible:

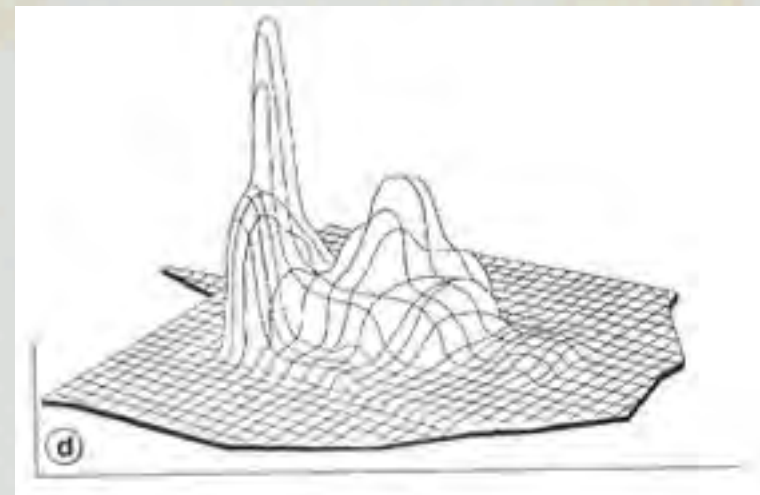
### Statistical surface:

3D representation of the data,  $z$  = numerical value of the attribute

**stepped** surface  
(choropleth map)



**continuous** surface  
(isoline map)



## Data classification

### Classification requirements:

2. The final map should display the patterns/structures, which are characteristic for the displayed phenomena. Extreme values should not disappear through classification method.
3. Each class should contain observed values.

### If these requirements are met:

- map gives a clear overview of the phenomenon,
- it is possible to determine value of the mapped attribute at every location on the map.

## Data classification

### Classification in 3 steps:

1. Choose a map type.
2. Limit the number of classes.
3. Define the class limits – the most difficult step.



Graphical methods

Break points  
Frequency diagram  
Cumulative frequency diagram

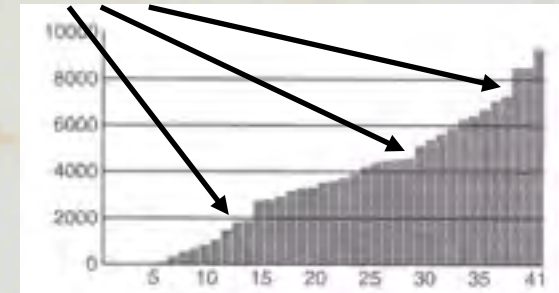
Mathematical methods

Equal steps  
Quantiles  
Arithmetic series  
Geometric series  
Harmonic series  
Nested means

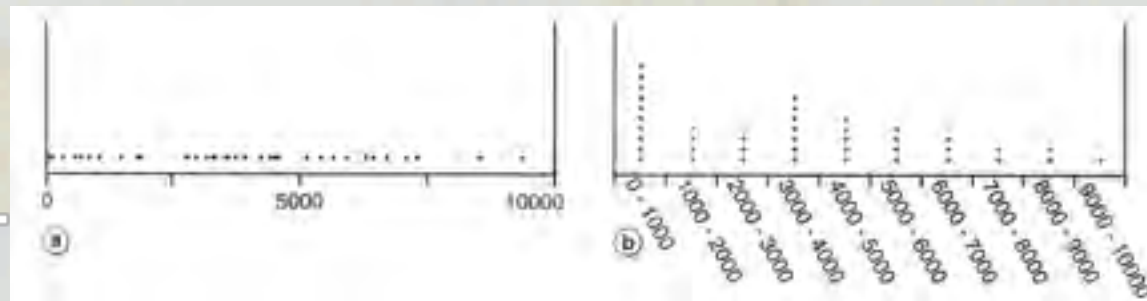
## Data classification

### Graphical methods of classification

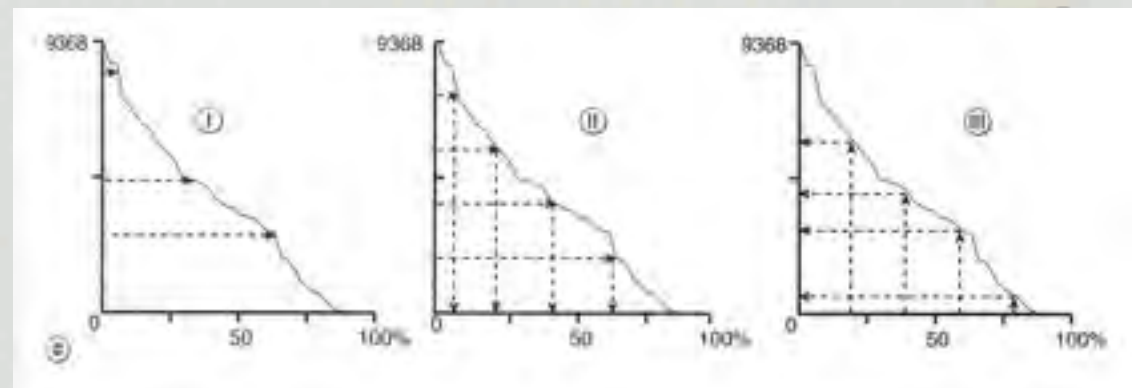
**Break points** – separate classes at points of discontinuities in the observation series



**Frequency diagram** – plot all frequencies, find discontinuities

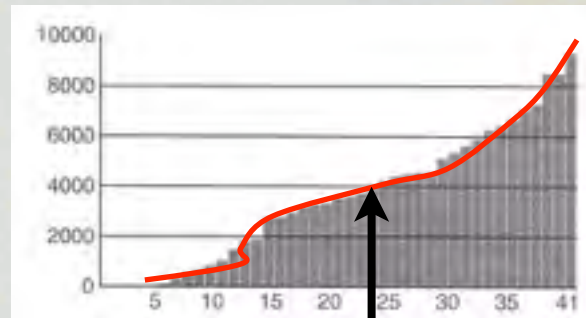


**Cumulative frequency diagram** – plot the added frequencies

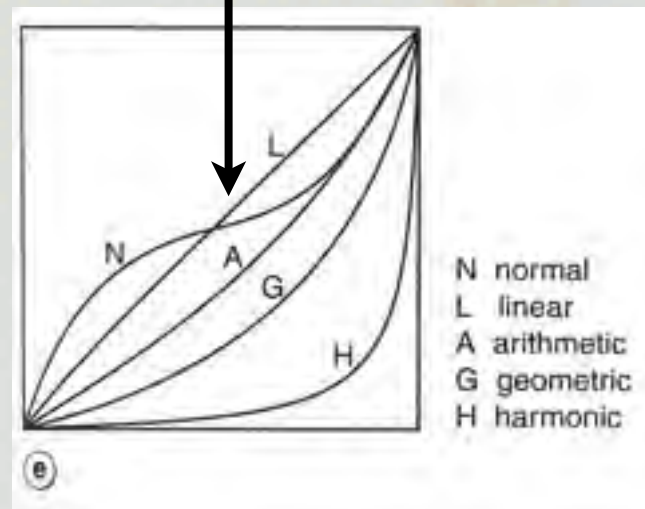


# Data classification

## Mathematical methods of classification

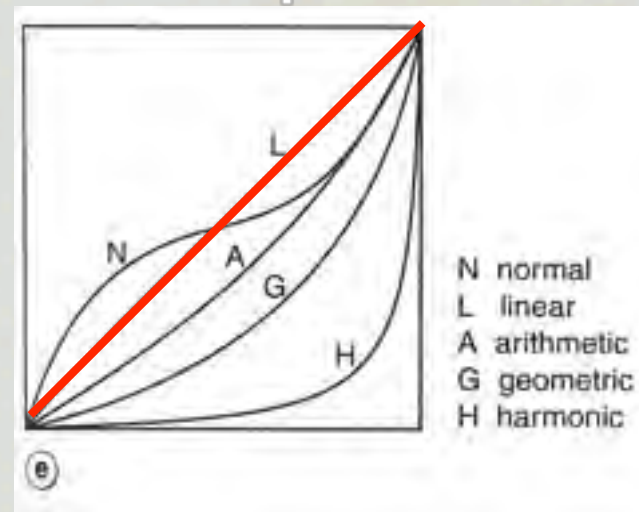


All methods draw a curve on top of observation series:  
the classification method is chosen according to this curve.



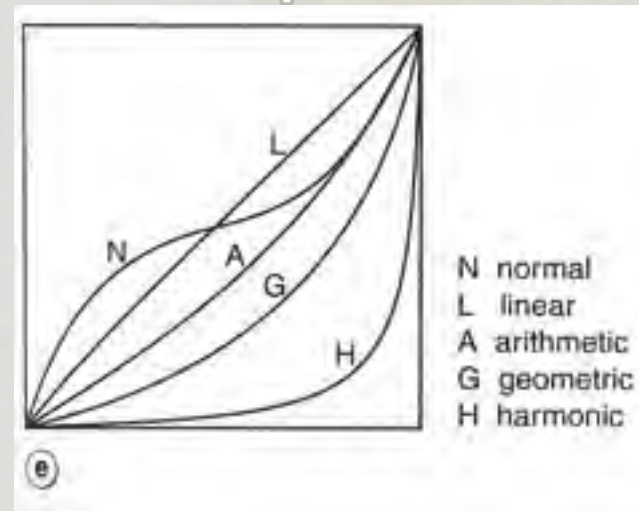
## Data classification

Linear curve L – **Equal steps classification** – equal width for all classes



## Data classification

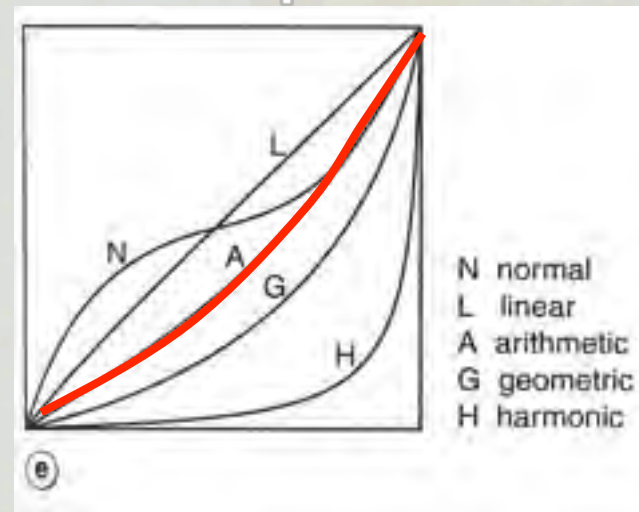
**Quantiles** – splits the number of observations proportionally over all classes. 4 classes: quartiles, 5 classes: quintiles, etc.





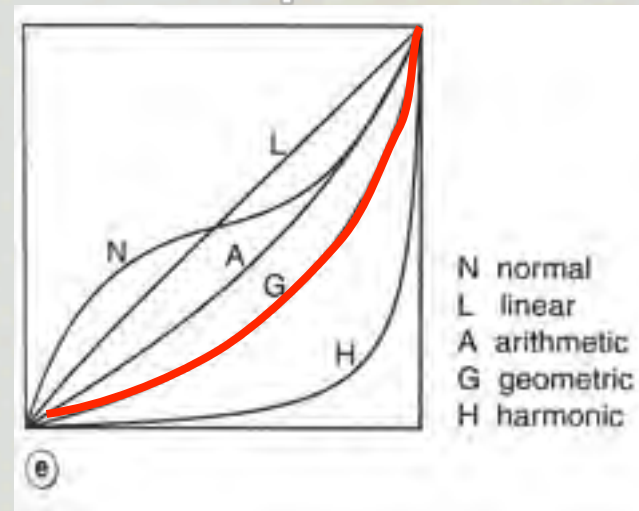
## Data classification

**Arithmetic series** – series  $a_1, a_2, a_3, a_4, \dots$ , where  $a_{n+1} = a_n + c$ ,  $c = \text{const}$ ,  
curve A



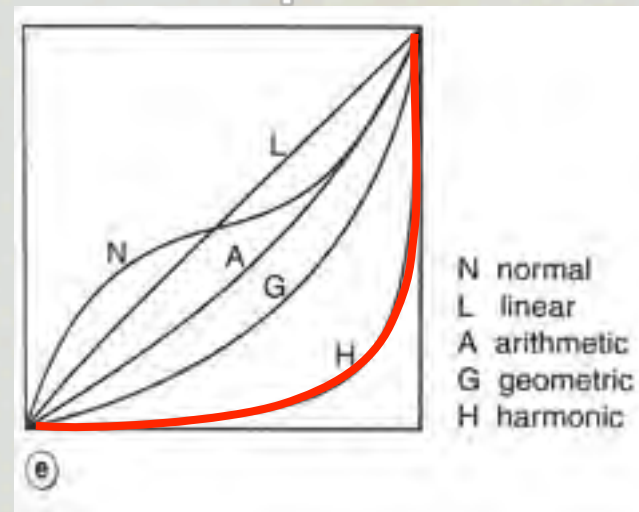
## Data classification

**Geometric series** – series  $a_1, a_2, a_3, a_4, \dots$ , where  $a_{n+1} = a_n * c$ ,  $c = \text{const}$ ,  
curve G



## Data classification

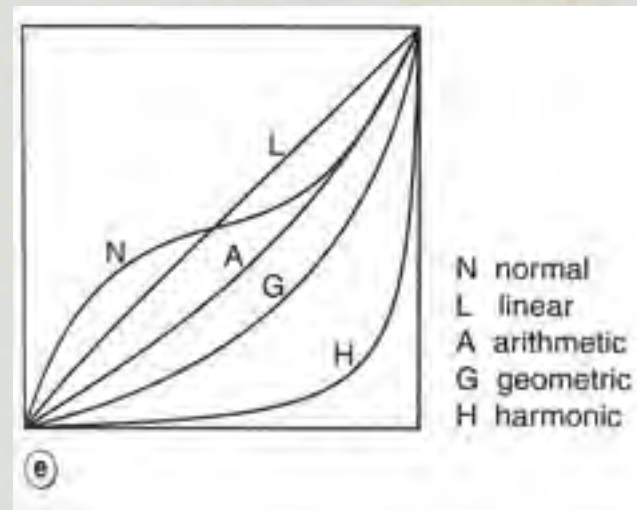
**Harmonic series** – reciprocal values of the attribute form an arithmetic series - series  $a_1, a_2, a_3, a_4, \dots$ , where  $1/a_{n+1} = 1/a_n + c$ ,  $c = \text{const}$ , curve H - gives a good classification of small values



## Data classification

### Nested means:

1. calculate average of all values,  $a$ , set  $a$  as one class boundary,
2. calculate average of all values  $<a$  and all values  $>a$ , set these two averages as class boundaries,
3. etc. until you reach the desired number of classes (always a multiple of 2.)



## Data classification

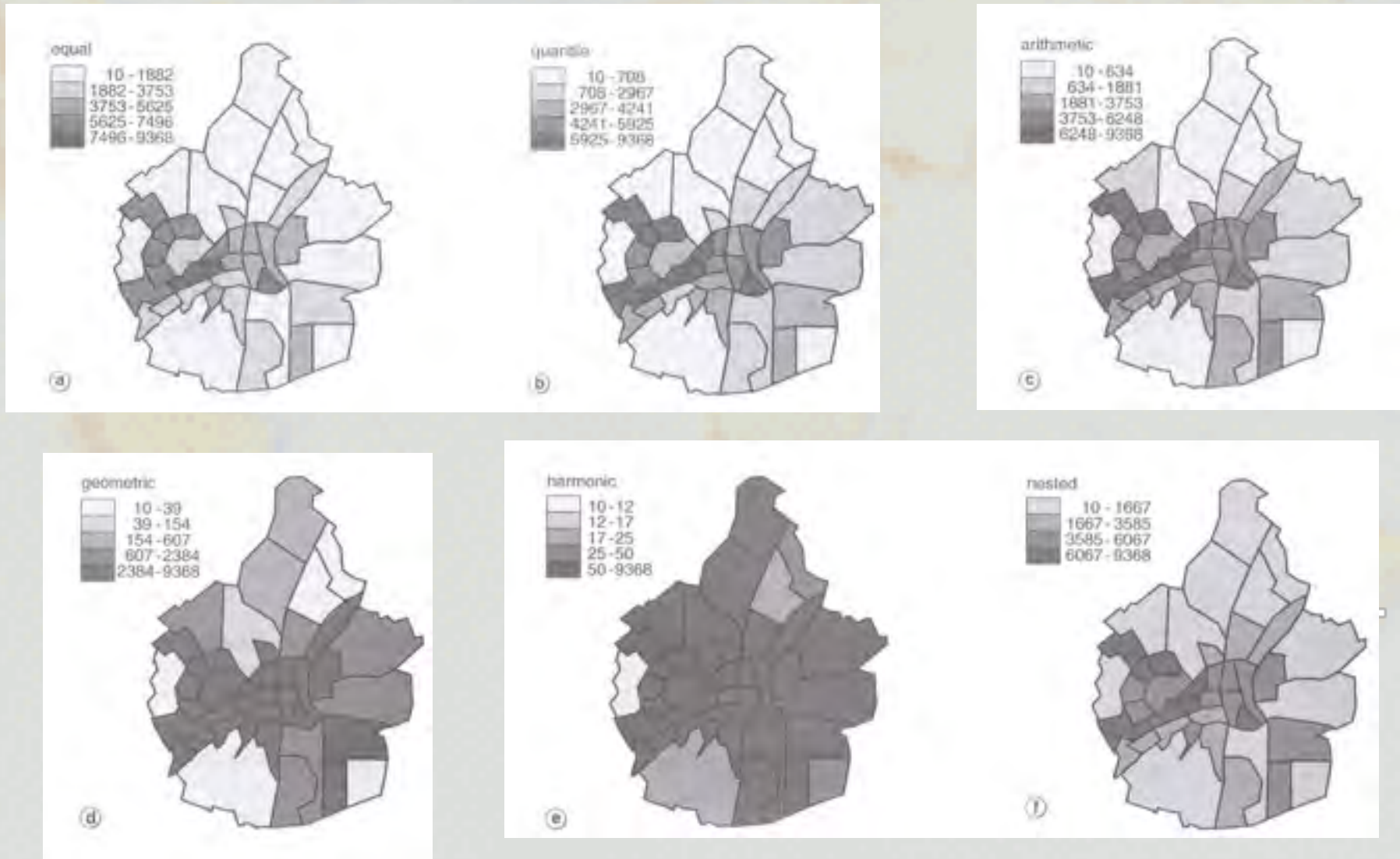
Every method results in different classifications:

equal	quantile	arithmetic	geometric	harmonic	nested
10 - 1882	10 - 708	10 - 634	10 - 39	10 - 12	10 - 1667
1882 - 3753	708 - 2967	634 - 1881	39 - 154	12 - 17	1667 - 3585
3753 - 5625	2967 - 4241	1881 - 3753	154 - 607	17 - 25	3585 - 6067
5625 - 7496	4241 - 5925	3753 - 6248	607 - 2384	25 - 50	6067 - 9368
7496 - 9368	5925 - 9368	6248 - 9368	2384 - 9368	50 - 9368	

(d)

## Data classification

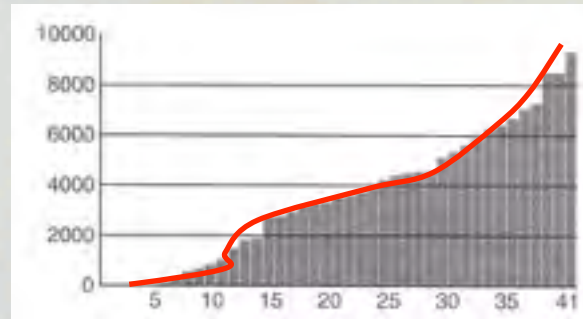
Every method results in a different map:



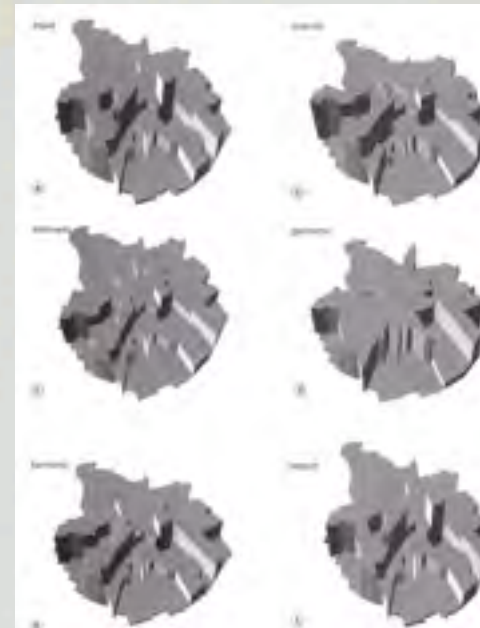
## Data classification

So, **which classification method is the best one?**

- the one that has the curve that best fits the observation series



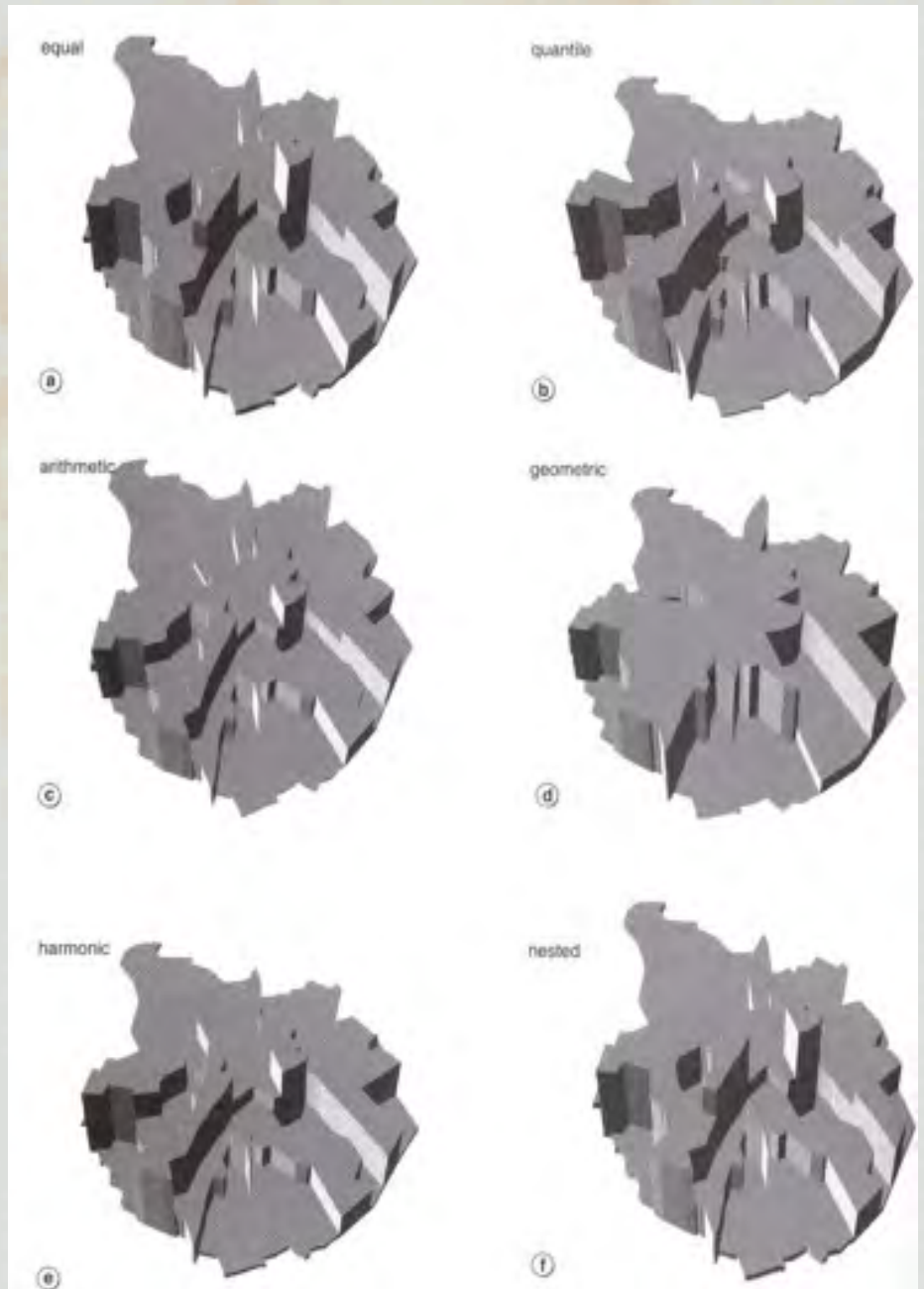
- or the one which produces the best-fitting statistical surface to the original statistical Surface:



# Data classification

Classified surfaces

Original surface





## Cartographical data analysis

Goal: to assess the characteristics of the components of the information and deciding which graphic variables to use for the visualisation.

**Step 1:** find the common denominator for all the data elements/  
categories selected for representation

→ The title of  
the map

Land	Apples	Pears	Prunes	Cherries	Other	Total
Saarland	30	10	20	10	10	80
Schleswig-Holstein	120	20	20	20	20	200
Hessen	130	20	40	30	10	230
Rheinland-Pfalz	120	30	40	40	10	240
Bavaria	210	40	50	30	10	340
Nordrhein-Westfalen	280	60	40	40	20	440
Lower Saxony	390	40	40	30	10	510
Baden-Württemberg	900	160	100	30	20	1210

Fruit production in Germany in 1967

## Cartographical data analysis

**Step 2:** assess **the data variables** that vary from one data element to another.

Example: soil map – the geographical location of each sample site, the various soil units

**Step 3:** assess **the measurement scale** of these variables, **the range** of the data and **the length** of variables (= the number of classes/ categories).

**Step 4:** assess **the information hierarchy** – which aspects are the most important ones, which are the least important, what data categories come in-between and in which order? Translate the information hierarchy into graphical hierarchy.

**Step 5:** construct **a preliminary visualisation** – shows trends, patterns, etc. that one should stick to during the actual mapping. Transformations are applied to this visualisation, depending on the audience and communication objectives.

## Mapping methods

**Mapping methods** = standardised ways of applying the graphic variables for rendering information components. They take into account:

- measurement scale
- nature of distribution of objects
- continuous/discrete distribution
- smooth boundaries or not

**The nine most common mapping methods:**

- chorochromatic maps or mosaic maps,
- choropleth maps,
- isoline maps,
- nominal point maps,
- absolute proportional maps,
- diagram maps,
- dot maps,
- flow line maps and
- statistical surfaces.

## Mapping methods

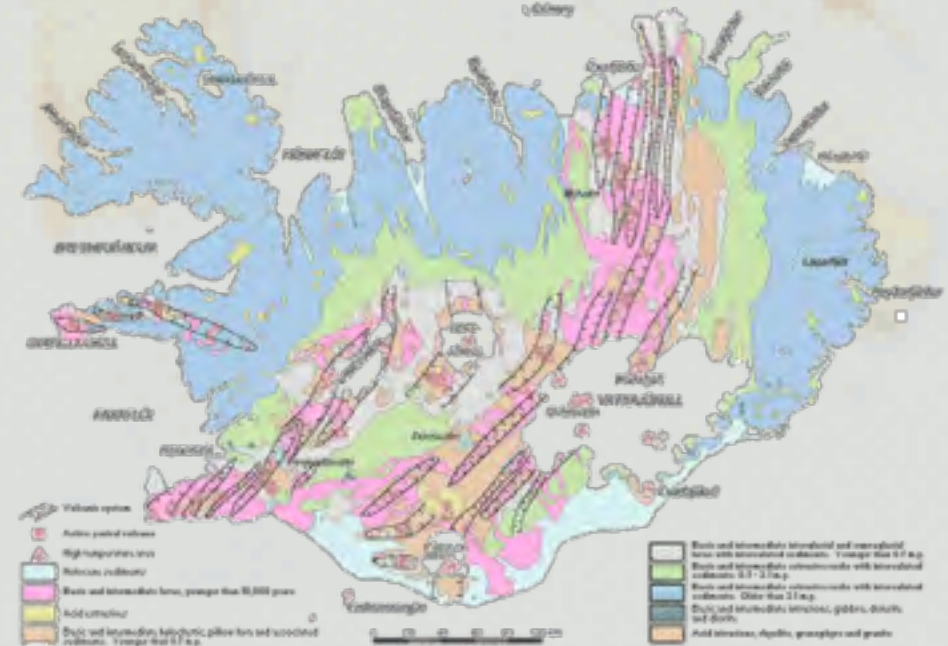
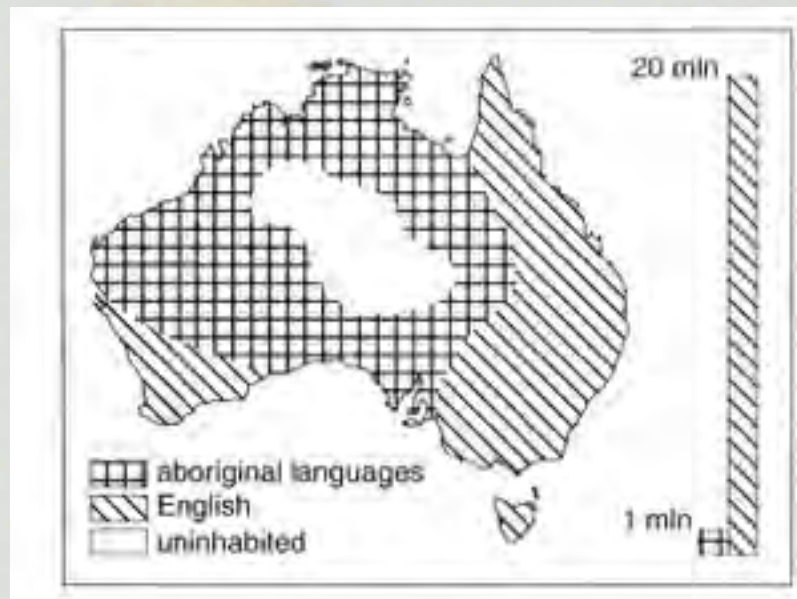
### Chorocromatic or mosaic maps

Greek: choros = area, chroma = colour



### Chorocromatic maps:

- rendering **nominal data (qualitative)** with the use of colours,
- or black and white patterns.



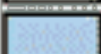




## Mapping methods

Important: only **nominal (qualitative) differences** shown!

↓  
NO hierarchy, NO order!

↓  
Different colours

	Basic and intermediate interglacial and supra-glacial lavas with intercalated sediments. Younger than 0.7 m.y.
	Basic and intermediate extrusive rocks with intercalated sediments. 0.7 - 3.1 m.y.
	Basic and intermediate extrusive rocks with intercalated sediments. Older than 3.1 m.y.
	Basic and intermediate intrusions, gabbro, dolerite and diorite
	Acid intrusions, rhyolite, granophyre and granite

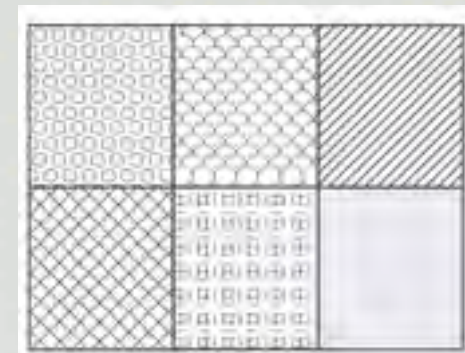
↓  
But: problems with perception:

- psychological values
- perception of one colour affected by surrounding colours
- saturated colours only for small areas (no domination)

Patterns

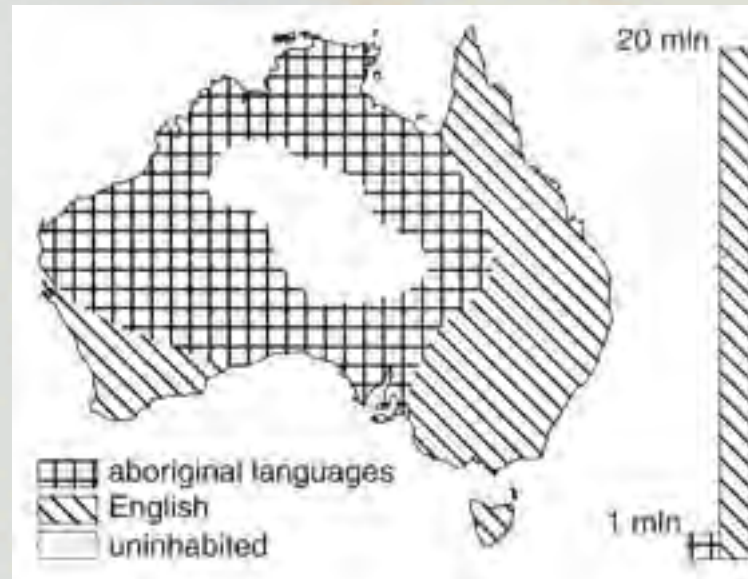
↓  
But:

- they have to be easily discernible one from another
- they have to be comparable (no domination) -> same grey value



## Mapping methods

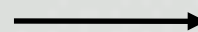
Influence of the area sizes, when non-area related phenomena are mapped:



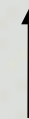
English speaking communities cover **the same area** as the aboriginal speaking communities.



Number of English speakers =  
number of aboriginal speakers



Correction: add a histogram with the number of speakers.



**Not true!** Outback is much more sparsely populated than the coastal area with predominately English speakers.

## Mapping methods

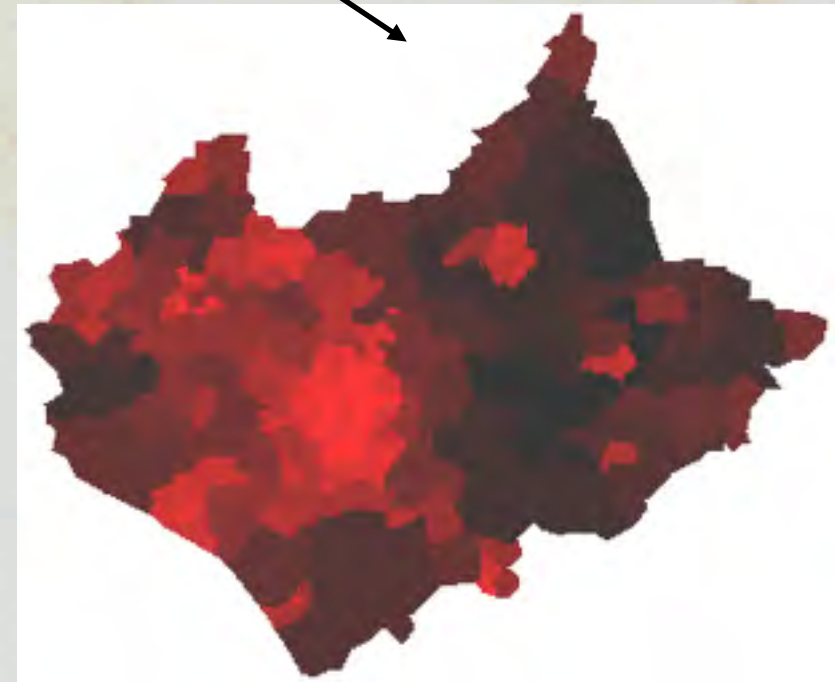
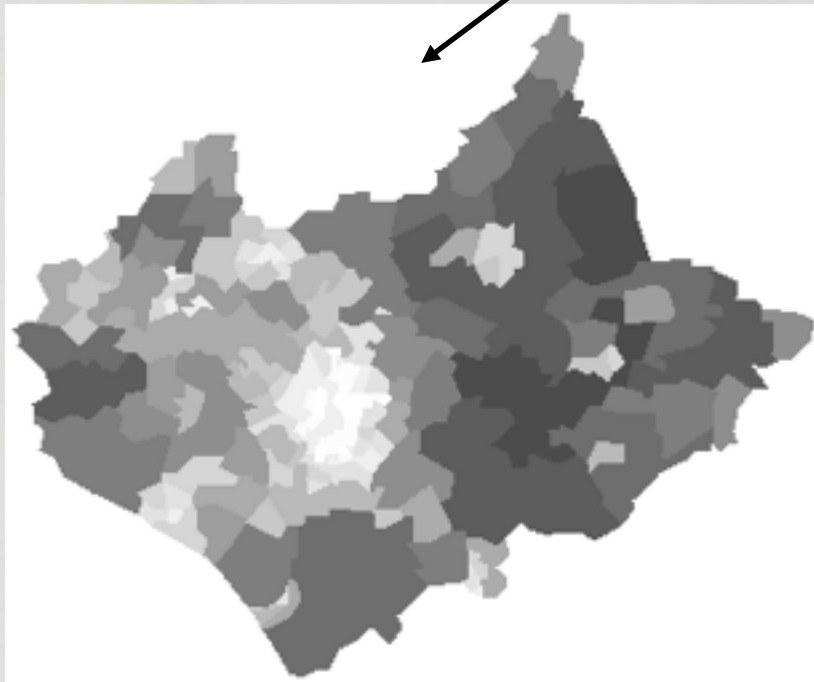
### Choropleth maps

Greek: choros = area, plethos = value



### Choropleth maps:

- rendering discrete **values (ordinal, interval, ratio data)**
- values calculated for areas and displayed as a stepped statistical surface
- using differences in **lightness (grey value)** or **saturation (chroma)** of a colour.



## Mapping methods

Differences in grey value / saturation



Differences in the intensity of the phenomenon: if correctly applied – percentage/density that is twice as high as another percentage/density, is represented by a twice as dark grey value.



Dark values: high intensity/density of the phenomenon

Light values: low intensity/density of the phenomenon

Hierarchy + order



## Mapping methods

### Two main types of choropleths



#### Density maps:

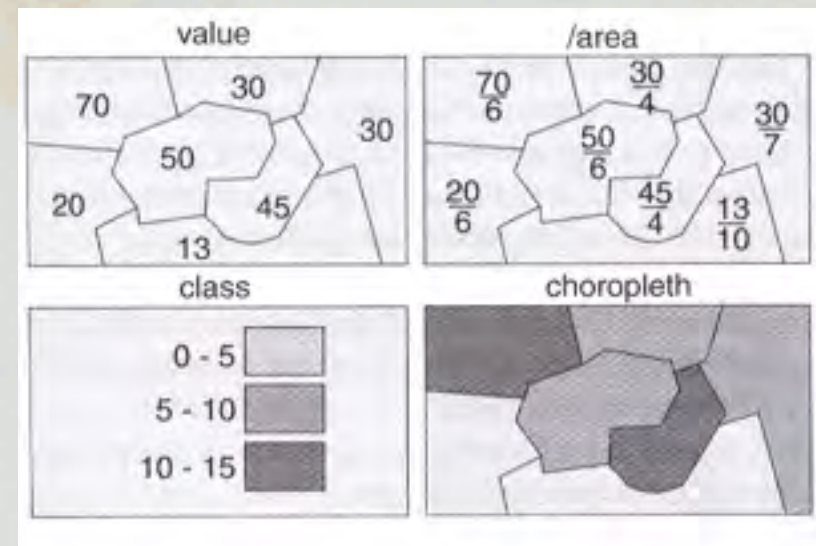
- ratio in which the areas covered are in the denominator

#### Non-area related ratio maps

Important difference for map-use: visual impression of a choropleth is affected by both the tint and the size of areas.

#### Production procedure for both types:

1. absolute value
2. put the absolute values into perspective
3. classification (max. 7 classes)
4. assigning grey values to classes



## Mapping methods

**Classification:** simplification of the image.

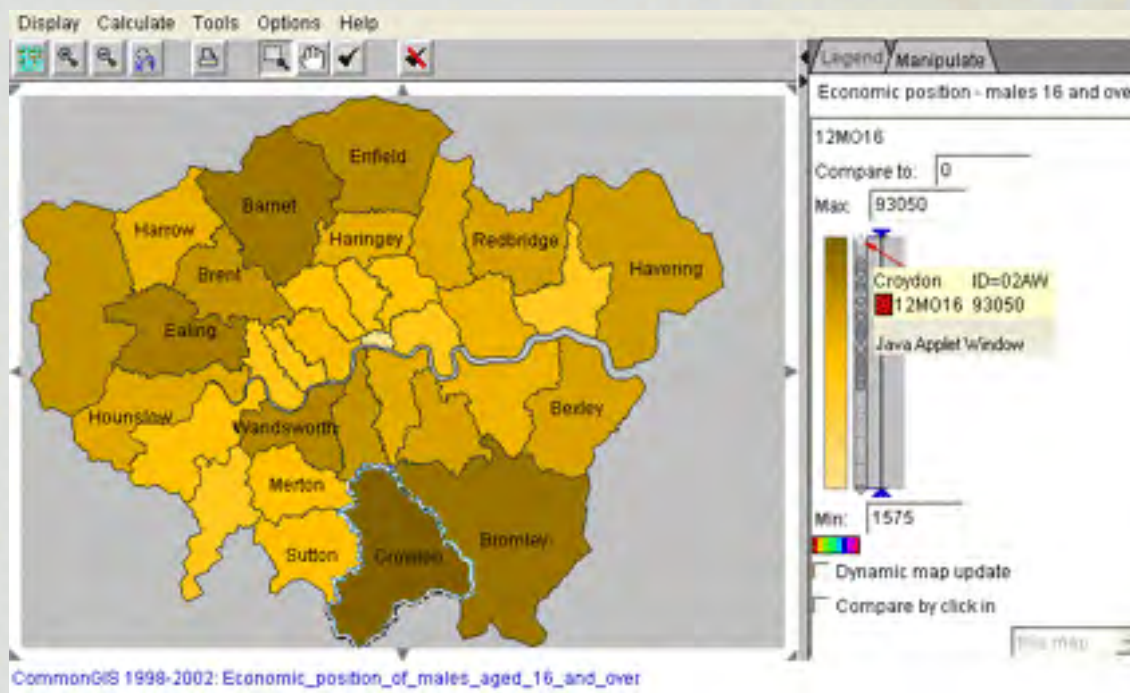
**Condition:**

minimal difference within classes + maximum difference between classes.



If the condition can't be met:

**unclassified choropleth map with a continuous scale**



## Mapping methods

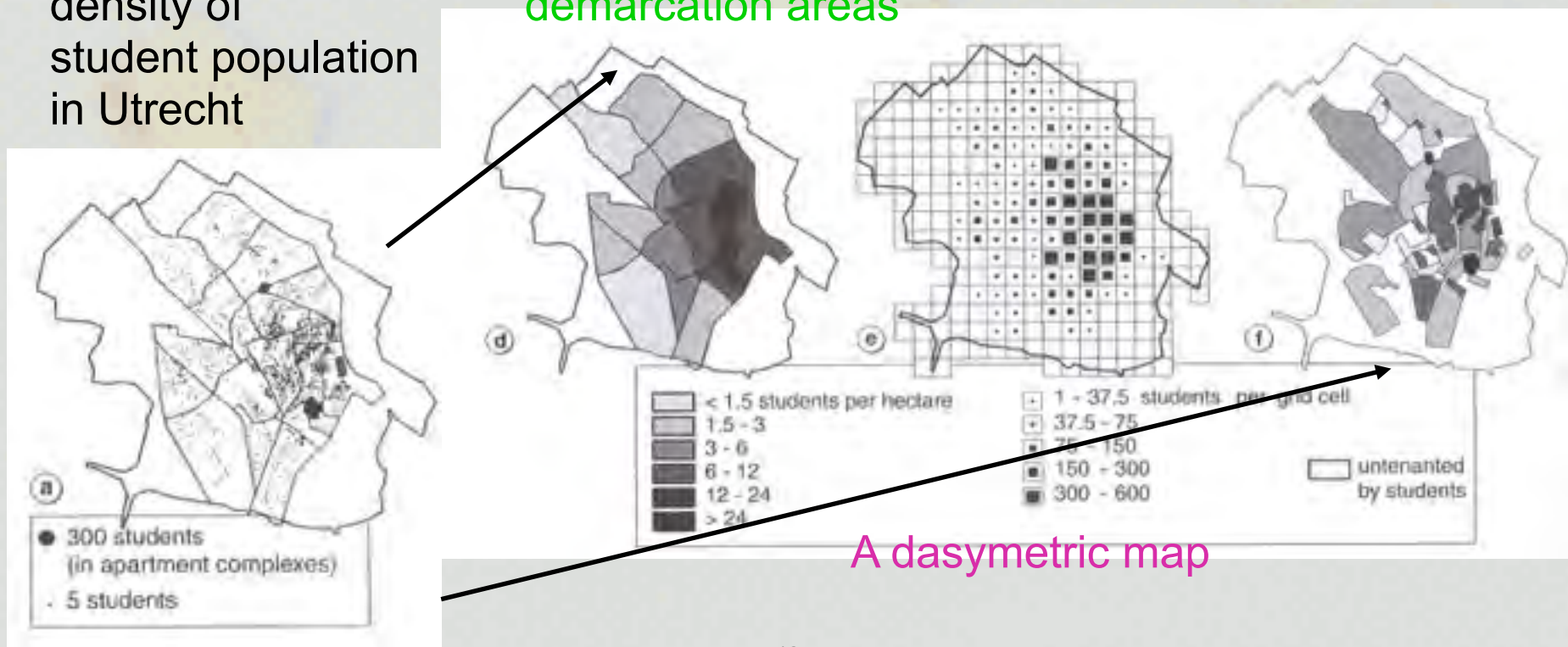
### A dasymetric map:

A choropleth map where **area boundaries** are adjusted to the occurrence of the phenomenon.

Usually: area boundaries are artificially created boundaries (I.e. administrative units or similar) that have nothing to do with the phenomenon.

A dot map of the density of student population in Utrecht

A choropleth with statistical demarcation areas

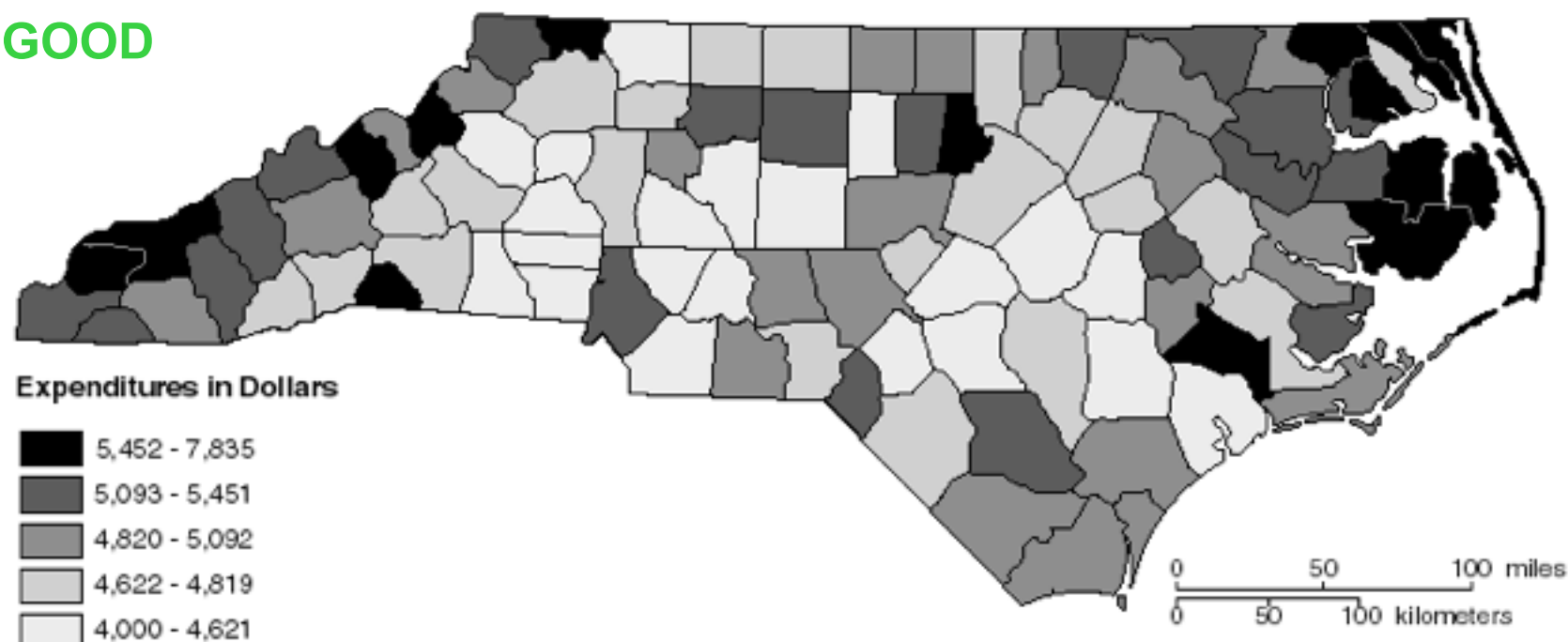


A dasymetric map

## Mapping methods

### Per Pupil Expenditure for Public Education in North Carolina, 1994-1995

GOOD



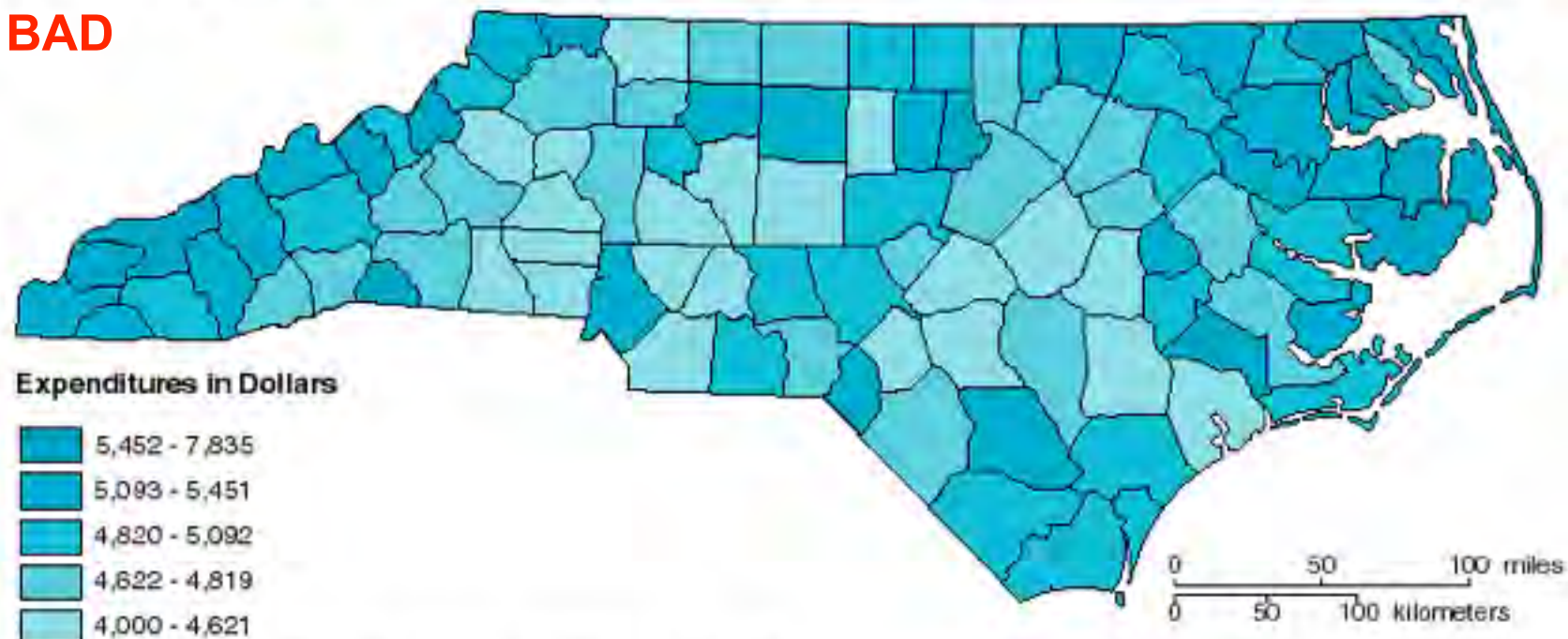
Source: NC Department of Public Instruction, *Statistical Profile*, 1996.

5 Classes can be represented sufficiently in black and white as well as by a single hue. The top class must be black and there must be at least 15% difference at the lower end of the value/chroma scale, at least 20% difference in the mid range and at least 25% for dark ranges. Percentages of black used here are: 8, 24, 50, 70 and 100%. Note that when adjacent polygons have black, the dividing lines are not visible when also in black. The polygon outlines must, in this case, be shown in a light gray or white. They are shown here in light gray where 2 or more adjacent counties are filled with black.

## Mapping methods

### Per Pupil Expenditure for Public Education in North Carolina, 1994-1995

**BAD**



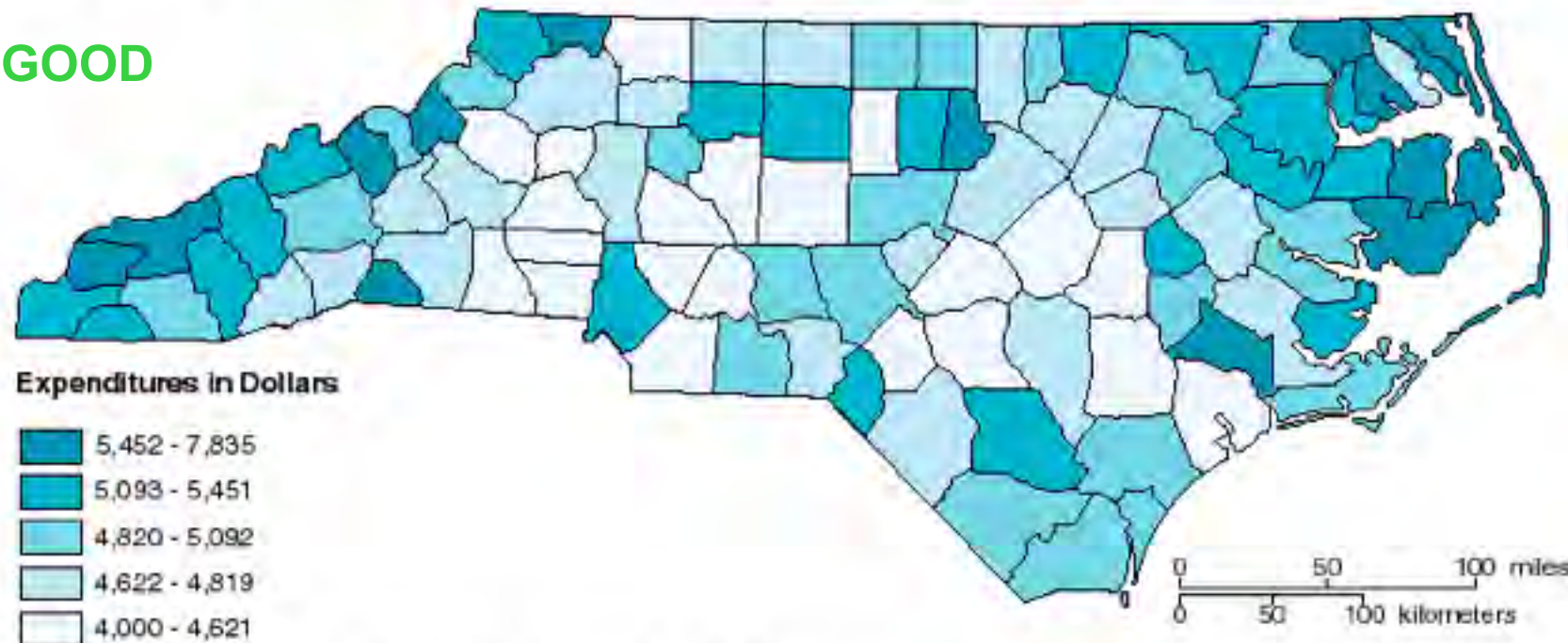
Source: NC Department of Public Instruction, *Statistical Profile*, 1996.

In this single-hue, 5-class choropleth map, the hue cyan is used to represent education expenditures. The percentage of cyan is varied ineffectively for providing a clear distinction between each class and for highlighting the highest data quantities. The percentages used are: 100, 85, 70, 55, and 40. A difference of 15% per step is not visually distinct enough to make for an effective single-hue series. There should be 20% or more difference in chroma (the amount of hue used, expressed in percent) between the darker hues in the single-hue series. At the lighter end of the scale, the lightest hue should be quite light (e.g., 10%) with at least 15 to 20% to the next hue for effective differentiation of low chroma hues. With 4 or fewer classes, it is not necessary to vary the value (i.e., no need to use black). But with 5 classes and a single hue, decreasing the value (adding small amounts of black) for the darkest hue helps with differentiation per hue and with highlighting the highest data quantities.

## Mapping methods

Per Pupil Expenditure for Public Education in North Carolina, 1994-1995

GOOD



Source: NC Department of Public Instruction, *Statistical Profile*, 1996.

Shown here is an example of a single-hue graded series for a 5-class choropleth map. Single-hue series' really work better for 4 or fewer classes but a single hue can be "stretched" to 5 distinct value/chroma steps by varying the percentage of the hue, and decreasing the value (adding black) of the hue for the highest data class. Percentages shown here are: 8, 24, 48, 80, and 100% Cyan with 10% Black added to the 100% Cyan. Percentages will vary depending on the hue used. Green works well for a 5-class single-hue graded series. Magenta, red, orange and brown can also form 5-class single hue series' but yellow would not work well.

## Mapping methods

Choropleth map = the prototypical thematic map

- most commonly used for portraying socio-economic data.

### Advantages:

- easy to produce and read,
- patterns are easy to recognize.

### Disadvantages:

- no variability within zones,
- boundaries of zones are often not related to phenomenon.

## Mapping methods

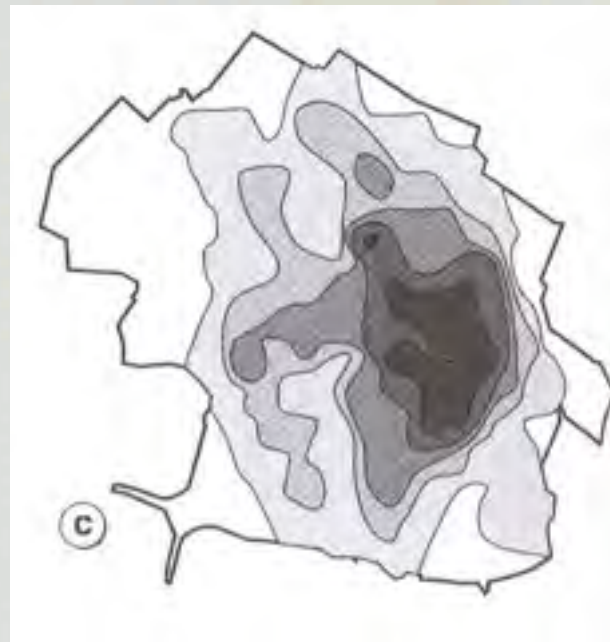
### Isoline maps

Greek: iso = equal



### Isoline maps:

- represent **continuous phenomena**
- **isoline** = a line which connects points with an equal value
- the data: measurement values that refer to points or areas

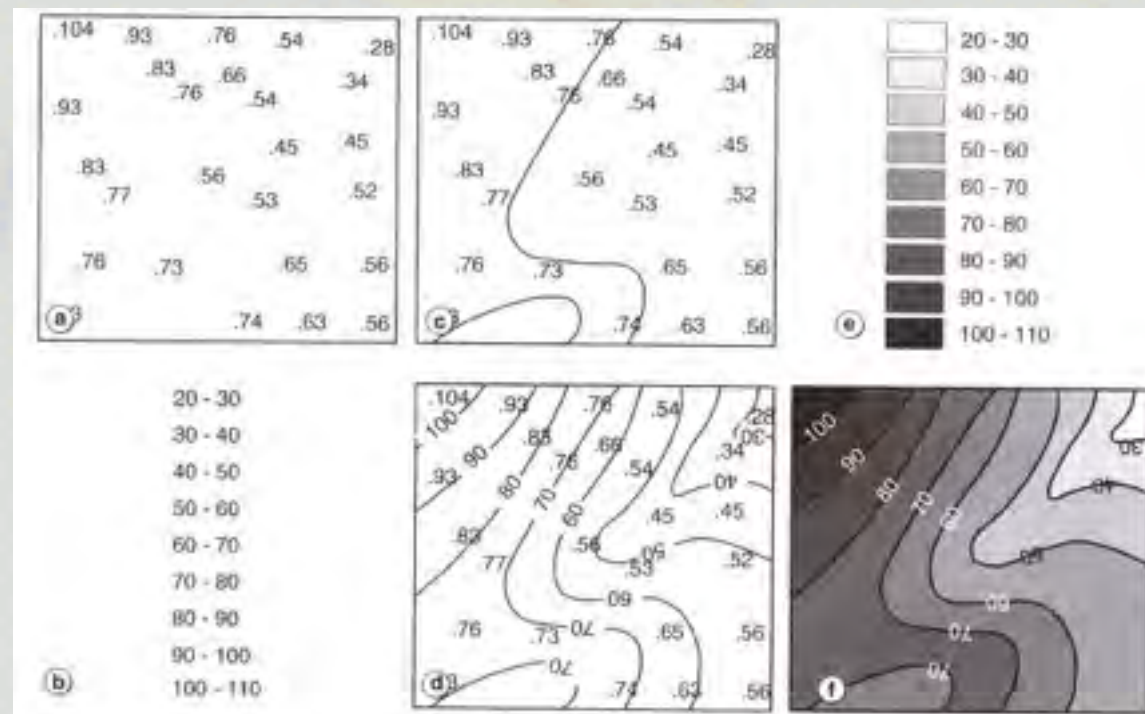




## Mapping methods

**Production procedure** for isoline maps with **point-based data**:

1. measure data in sampling points
2. categorise the data in classes
3. draw class boundaries by interpolation
  - construct the points that “have” the class boundary value
  - connect these points -> **isolines**
4. Add tints in-between isolines to better perceive the general trend.



## Mapping methods

**Production procedure** for isoline maps with **area-based data**:

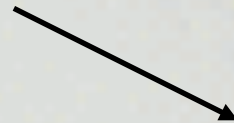
1. cover the areas with a grid and assign the appropriate values to each grid cell
2. – 4. same steps as for point-based data.



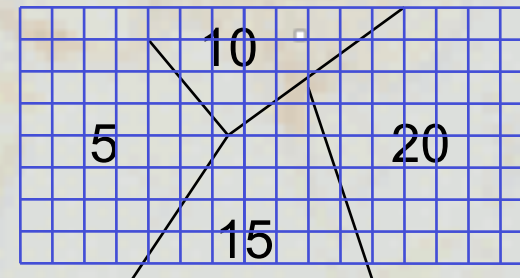
These maps are called:



**Pseudo isoline maps**  
(Europe)



**Isopleth maps**  
(UK)



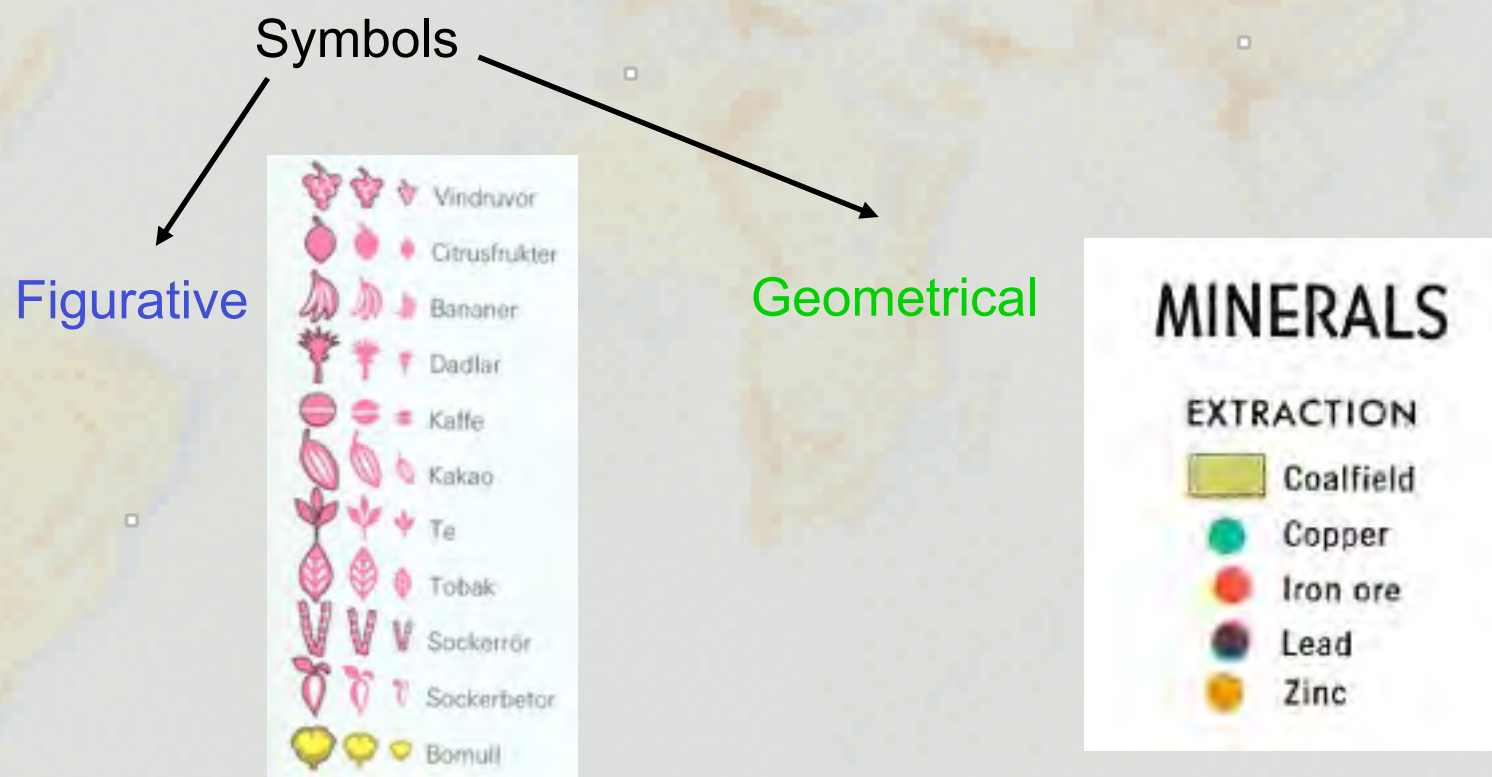
Isoline maps show **trends**:

- in which direction the values of the phenomenon are increasing/decreasing
- comparison between different phenomena and finding correlations between them.

## Mapping methods

### Nominal point maps

- representing **nominal data valid for point locations**
- by symbols, different in shape, orientation or colour.

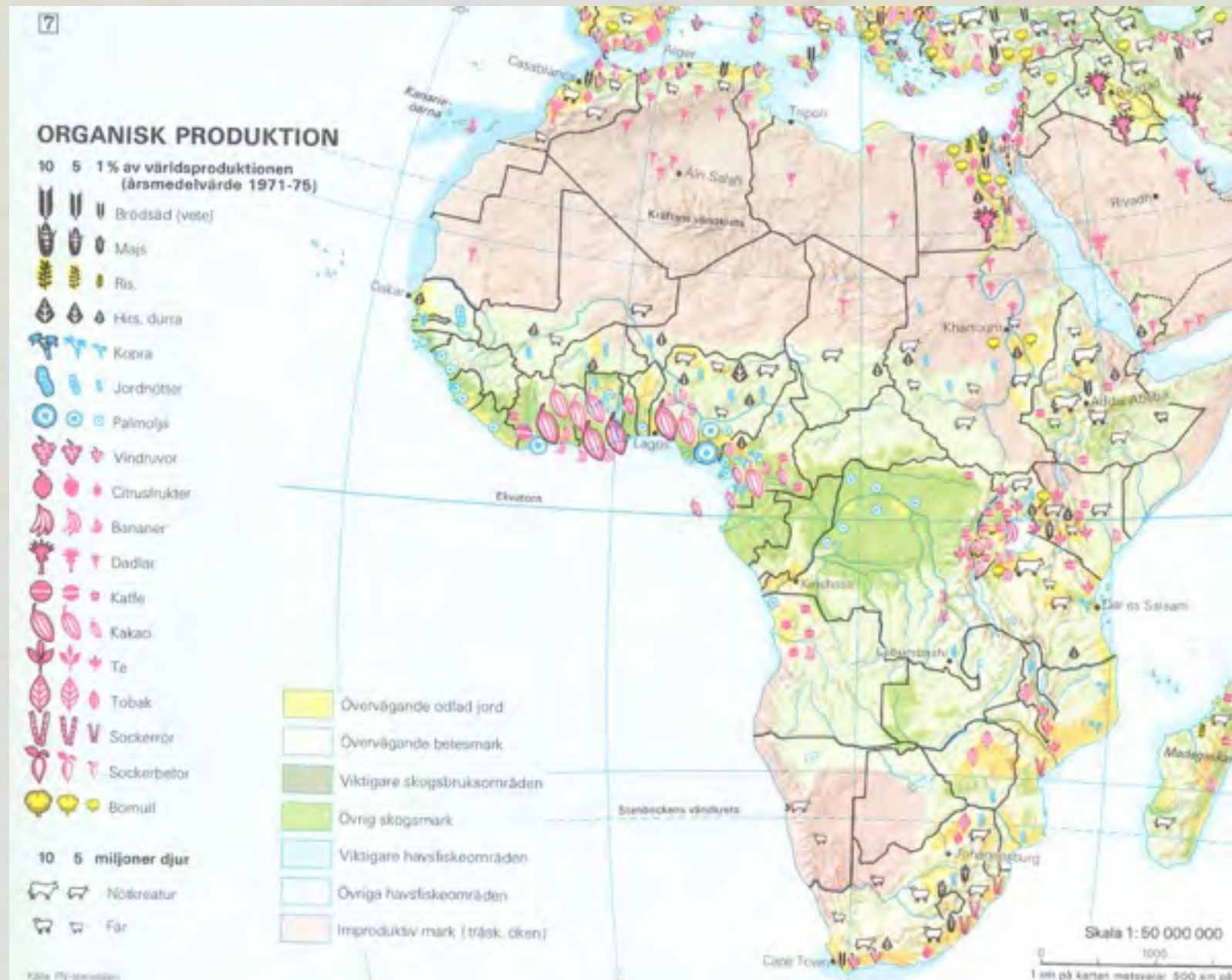


Easy recognition,  
difficult legibility of  
complex symbols

Less easy recognition,  
better legibility

# Mapping methods

## Figurative symbols



# Mapping methods

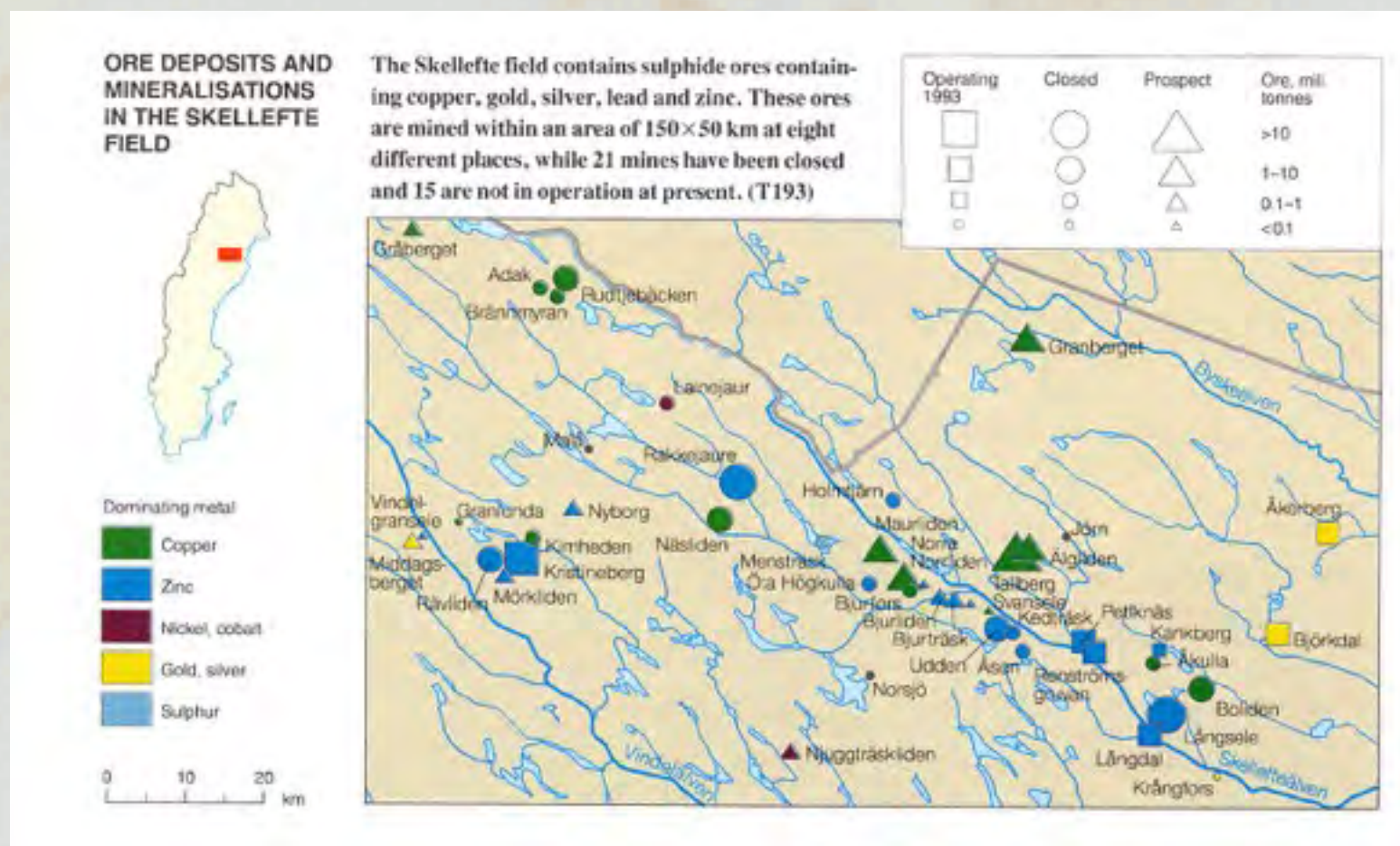
## Geometrical symbols



## Mapping methods

### Absolute proportional maps

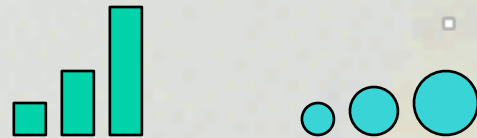
- representing discrete absolute values valid for point locations
- by geometrical symbols, where the size of the symbol represents the value of the attribute.



## Mapping methods

### Requirements:




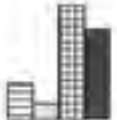
- **legibility** – depends on symbol density and contrast
- **comparability** – depends on the shape of symbols
  - > easier to compare sizes of symbols that grow in one direction than circles



**The range:** the ratio of the highest and lowest value that can still be represented proportionally without impairing legibility.

Effectiveness of different diagrams:

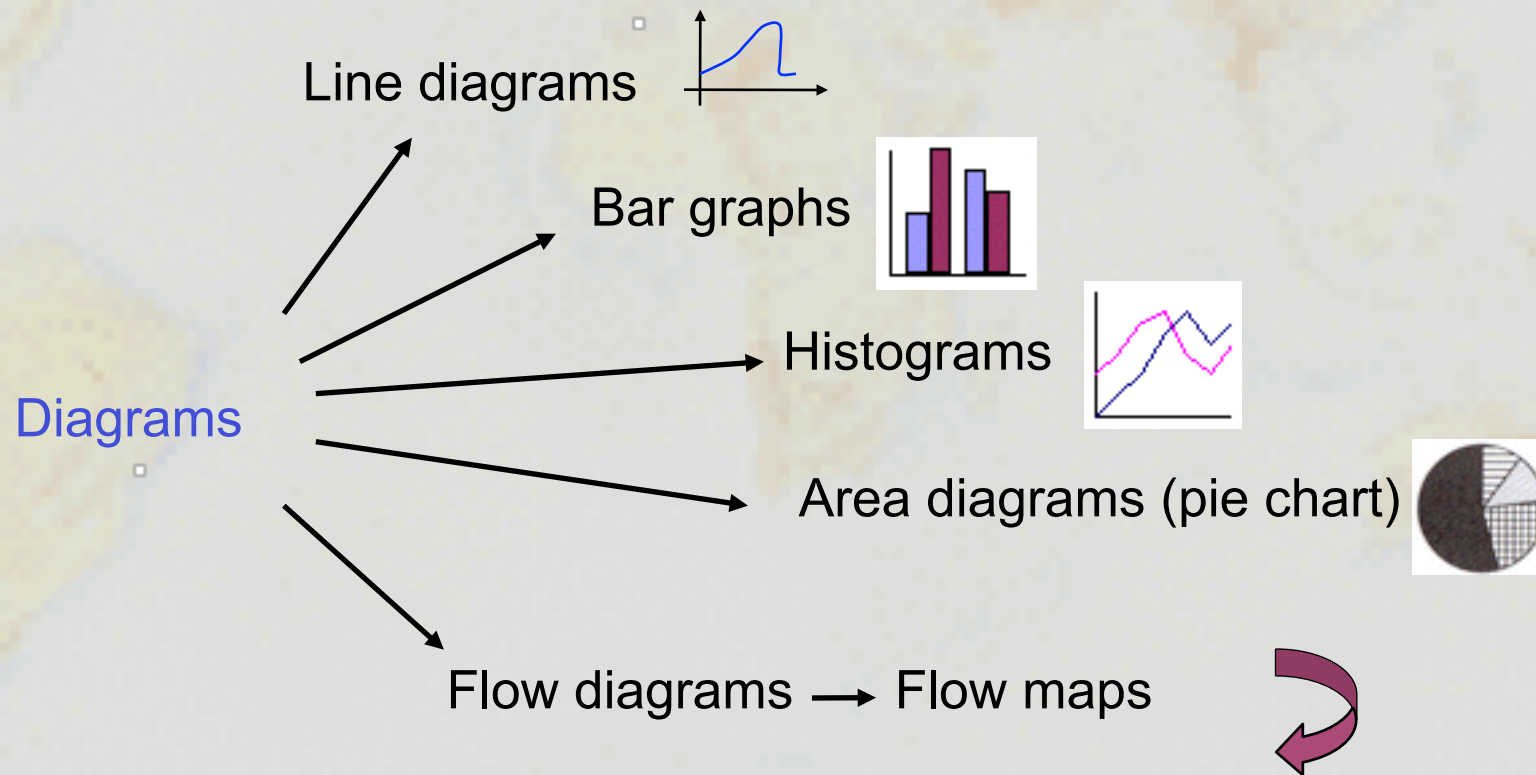
- (a) within each figure
- (b) between figures

name	shape	max. range
pie chart		a) 1:275 b) 1:2500
pie chart with different scales		a) 1:140 b) 1:1400
bar graph		a) 1:5 b) 1:100
histogram		a) 1:10 b) 1:100

# Mapping methods

## Diagram maps

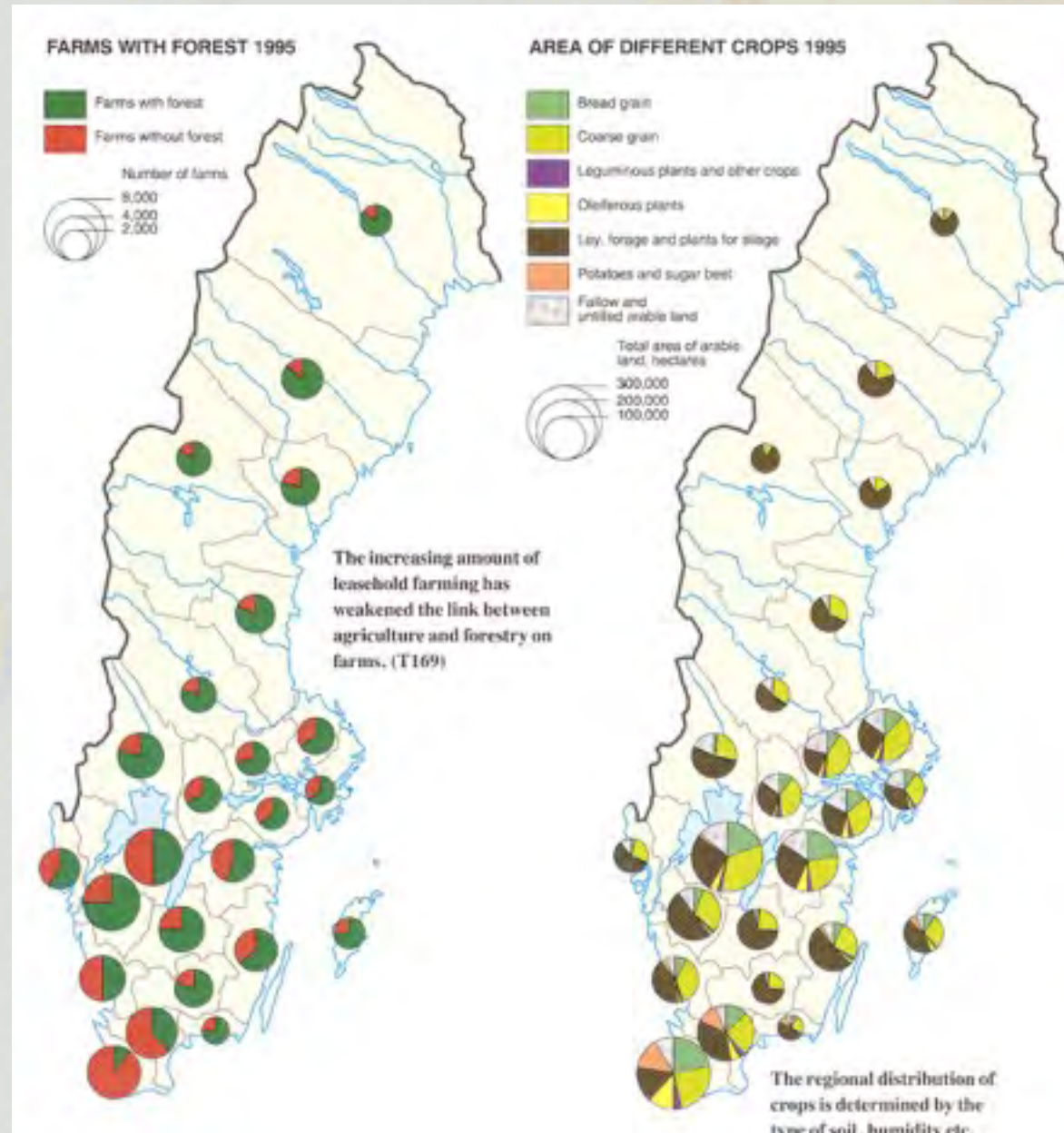
- maps that contain diagrams





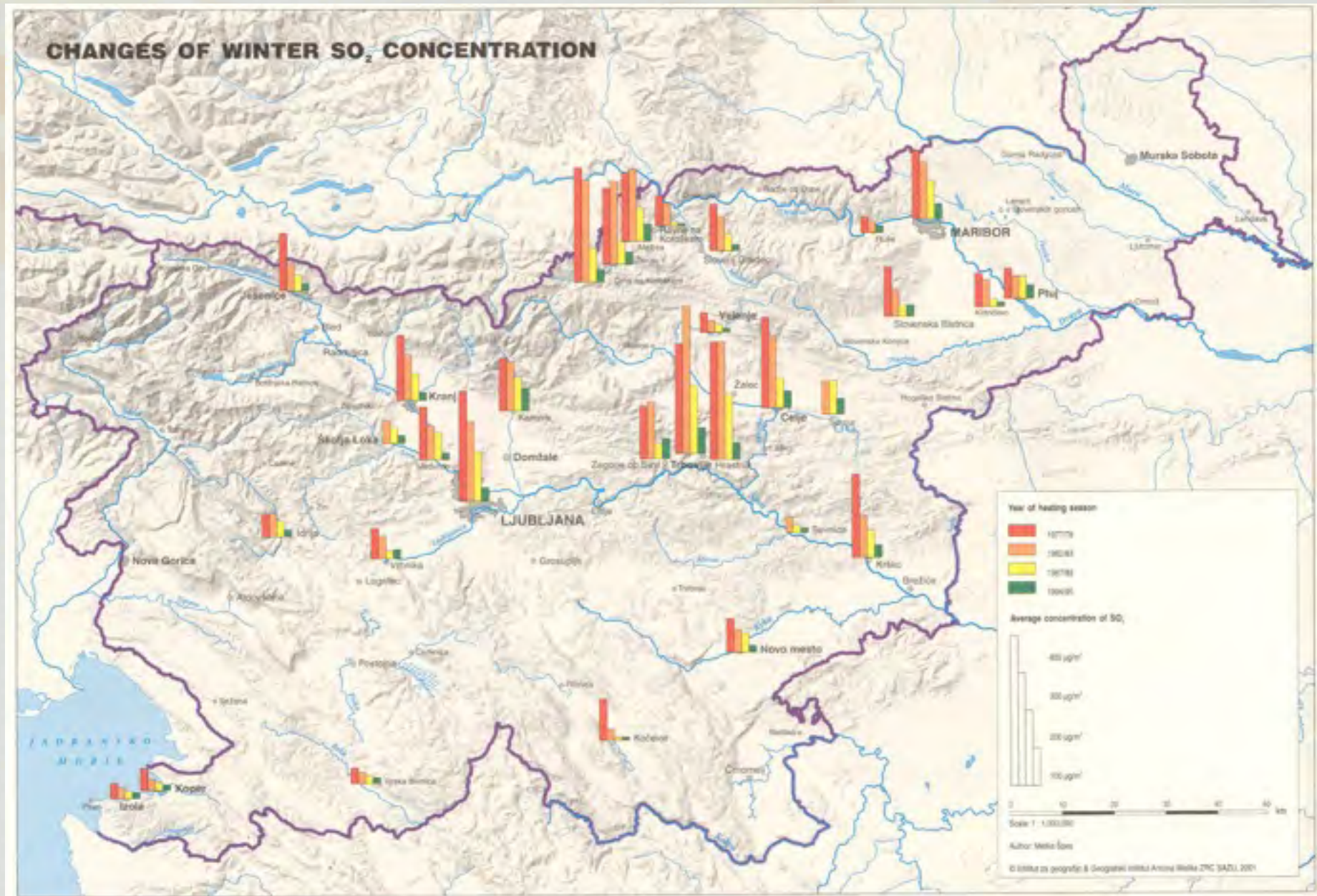
# Mapping methods

## Pie chart maps



# Mapping methods

## A bar chart map



## Mapping methods

### Dot maps

- a special case of proportional symbol maps
- represent point data through symbols that each shows the same quantity and is located as near the actual location as possible
- show patterns



## Mapping methods

### Flow maps

- simulate **movement** by:
  - using graphical variables that give an ordered impression
  - by showing a number of situations adjacent in time
  - by using symbols, associated with movement



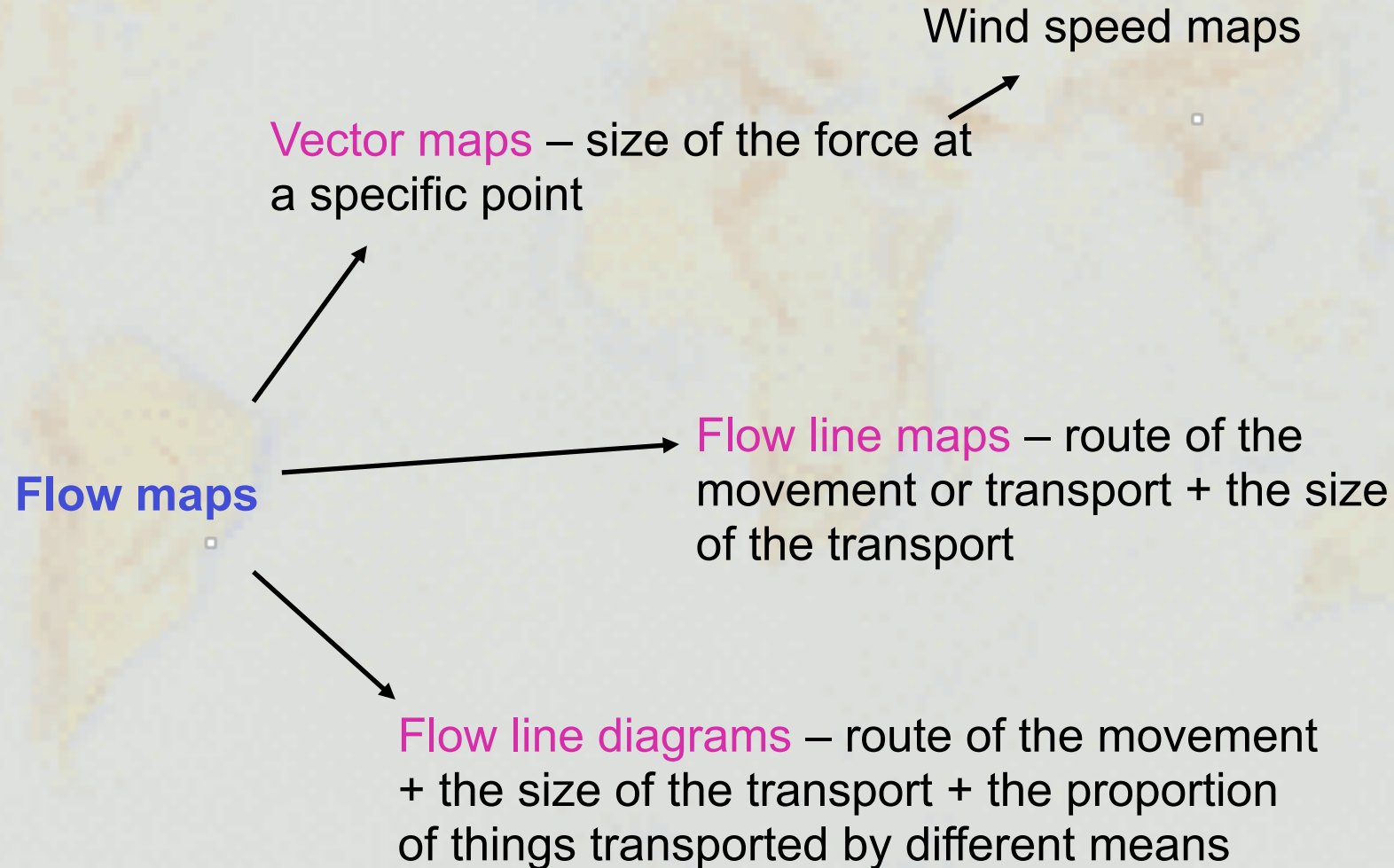
arrows

the route  
of the  
movement

the direction  
of the  
movement

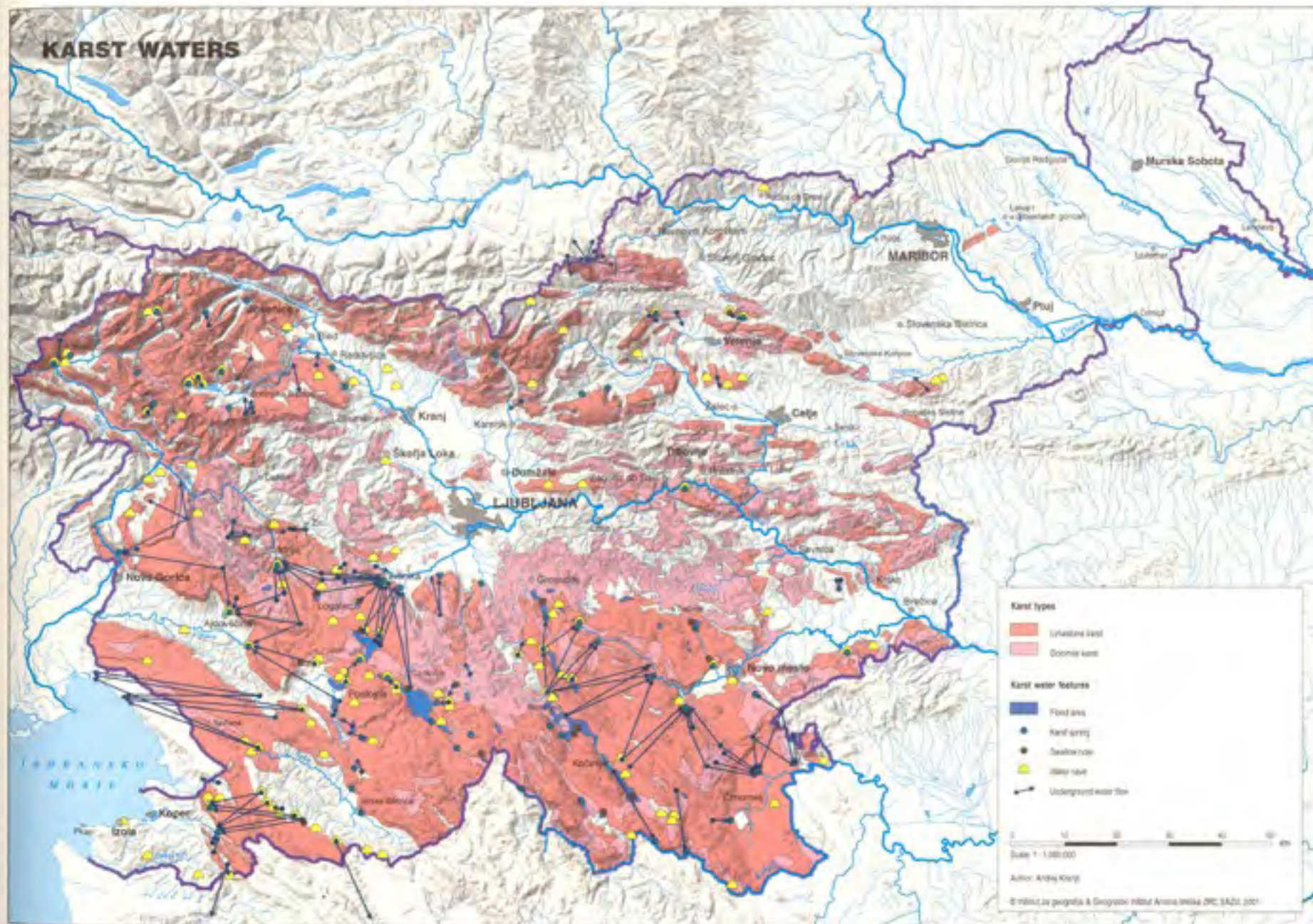
the volume  
transported

## Mapping methods



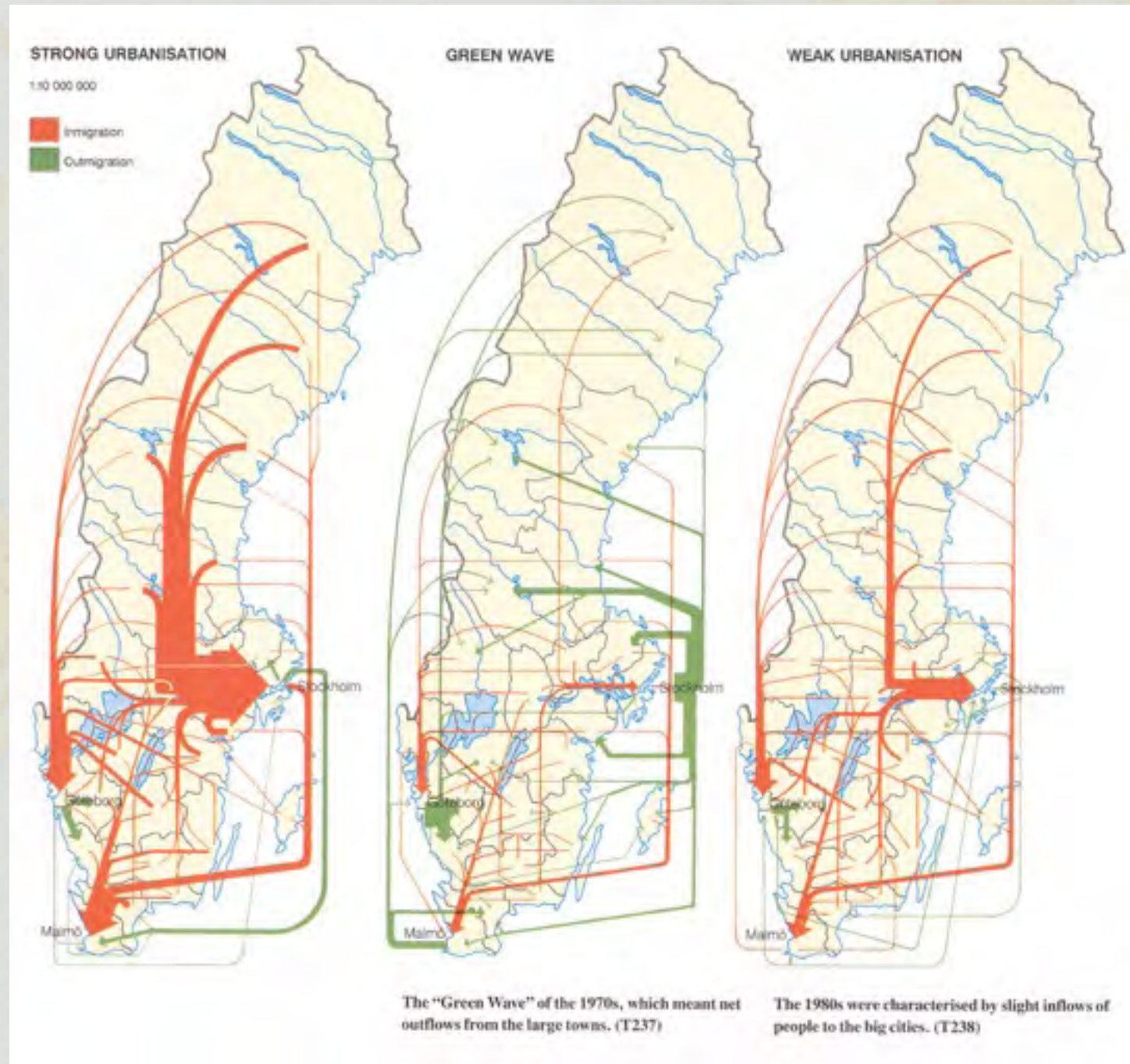
# Mapping methods

## A vector map



# Mapping methods

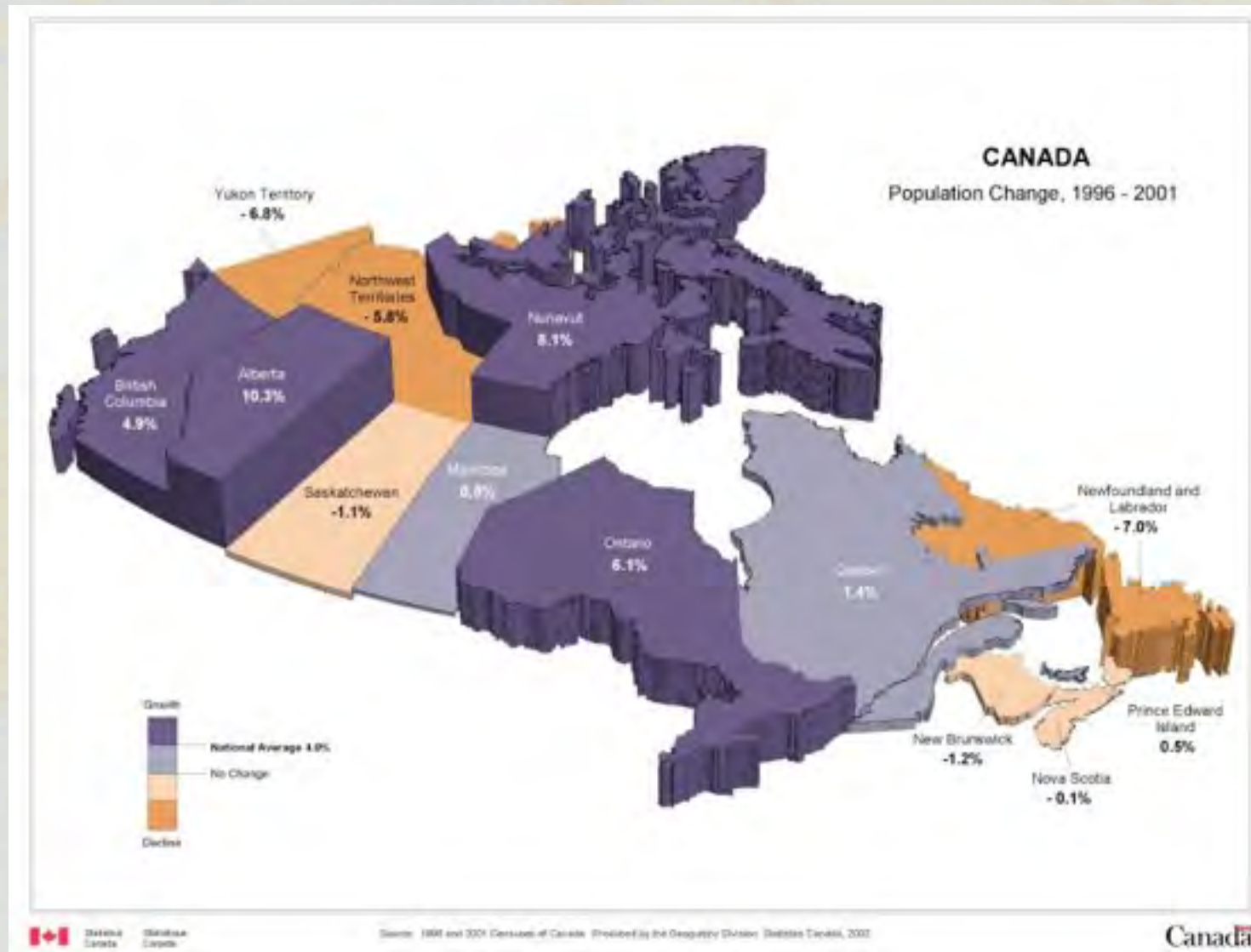
## Flow line maps



# Mapping methods

## Statistical surfaces

- 3D representation of quantitative data (as in isoline/choropleth maps)



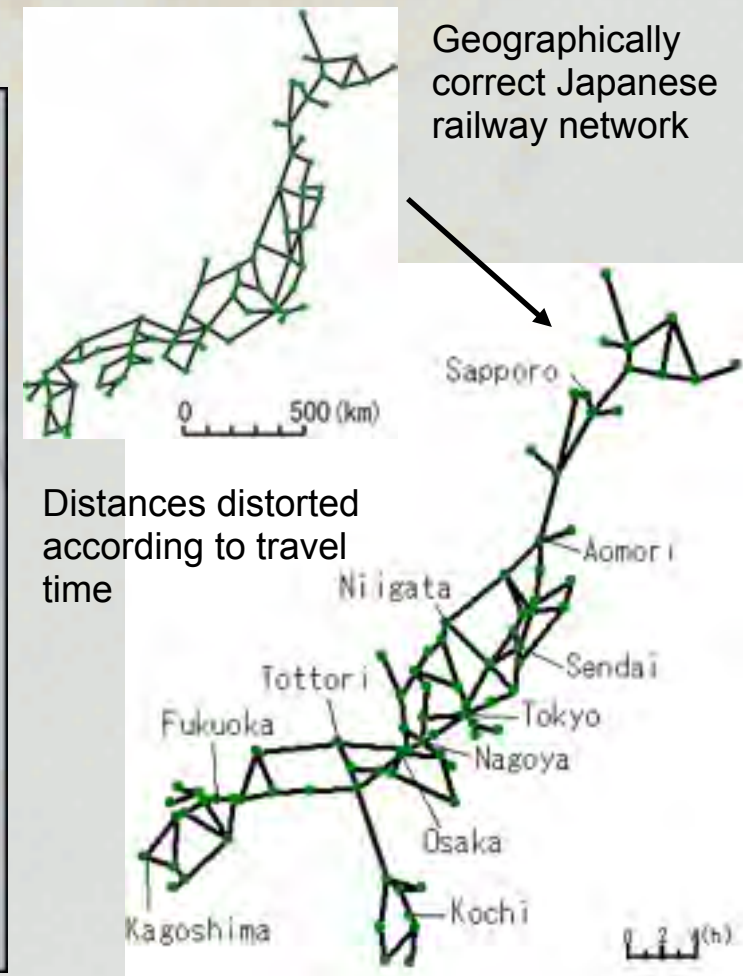
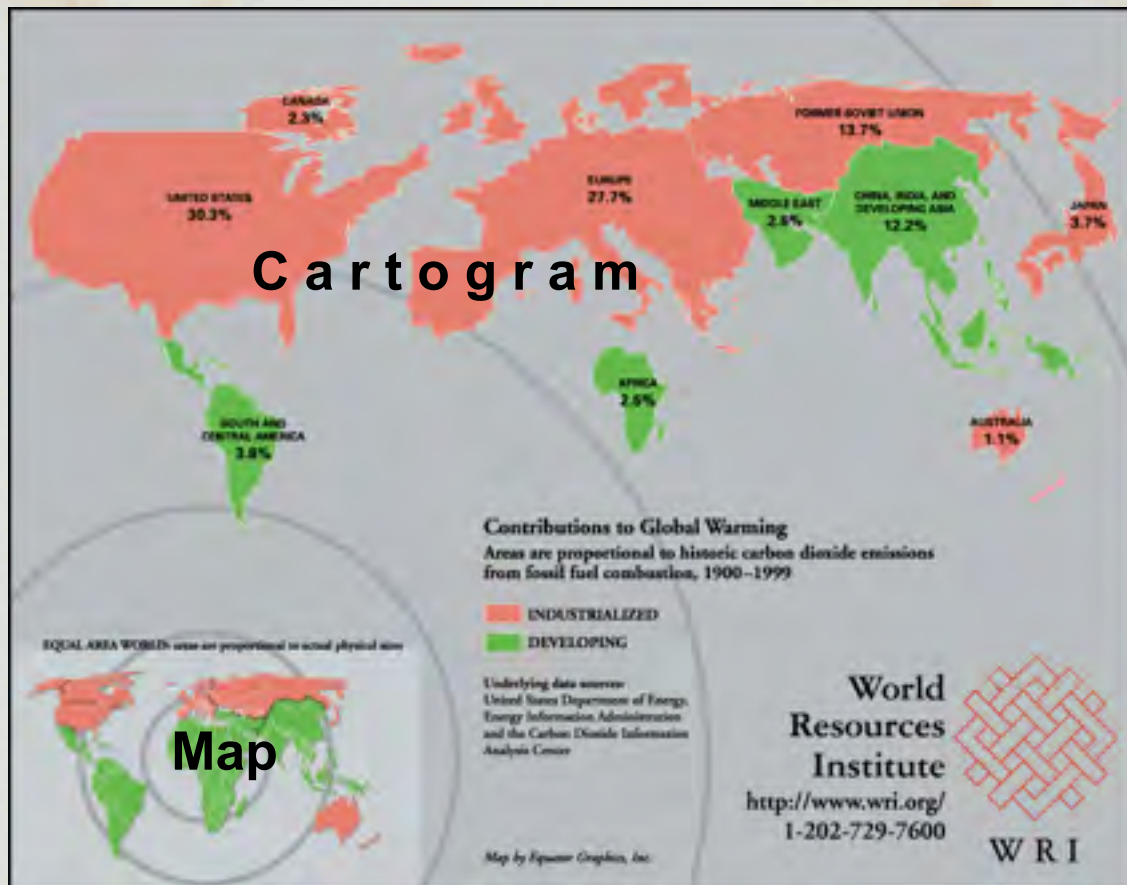


## Mapping methods

### Cartograms

Not proper maps! The geographical positions of objects are distorted in order to better show the observed phenomenon.

A **cartogram** is a generalization of an ordinary thematic map, which is **distorted** by resizing its regions according to a geographically-related input parameter.



## Mapping methods

**Area cartogram:** the area of each polygon represents some numerical attribute of the polygon (in this case the population).





# Mapping methods

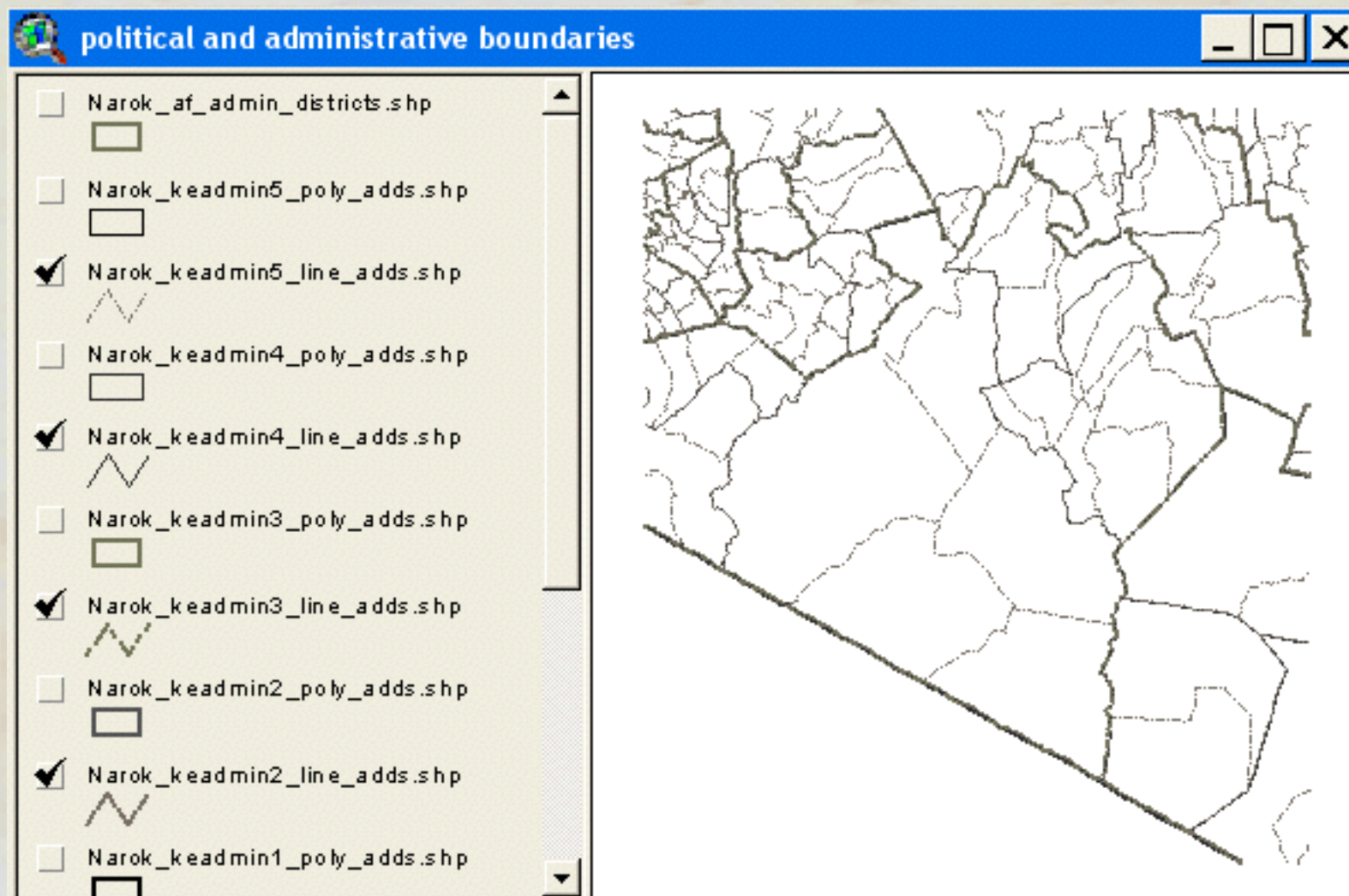
A linear cartogram: shows the location of the stations in relation to the public traffic train network in Stockholm



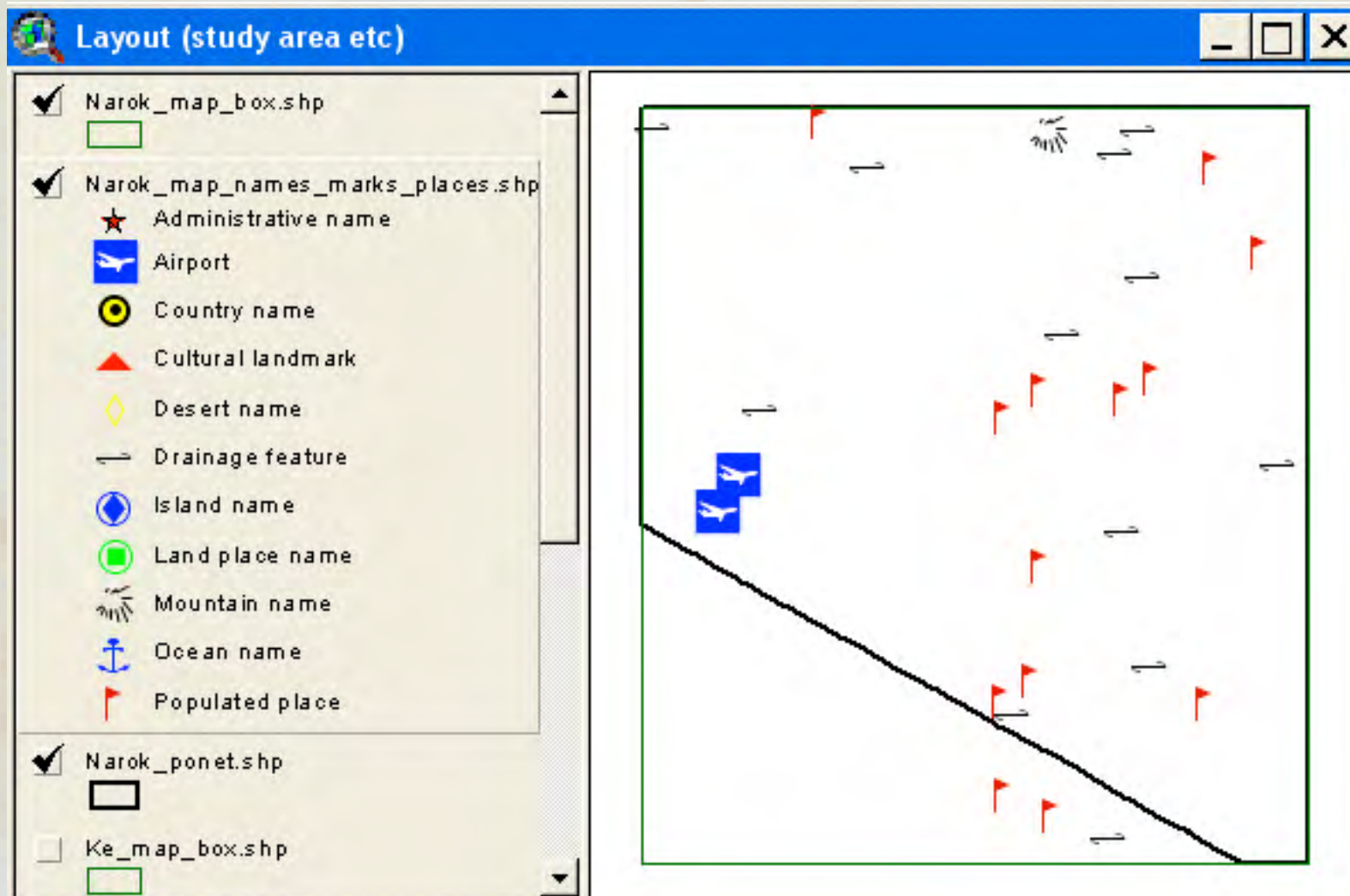
$d_1 = d_2 < d_3$  Really????



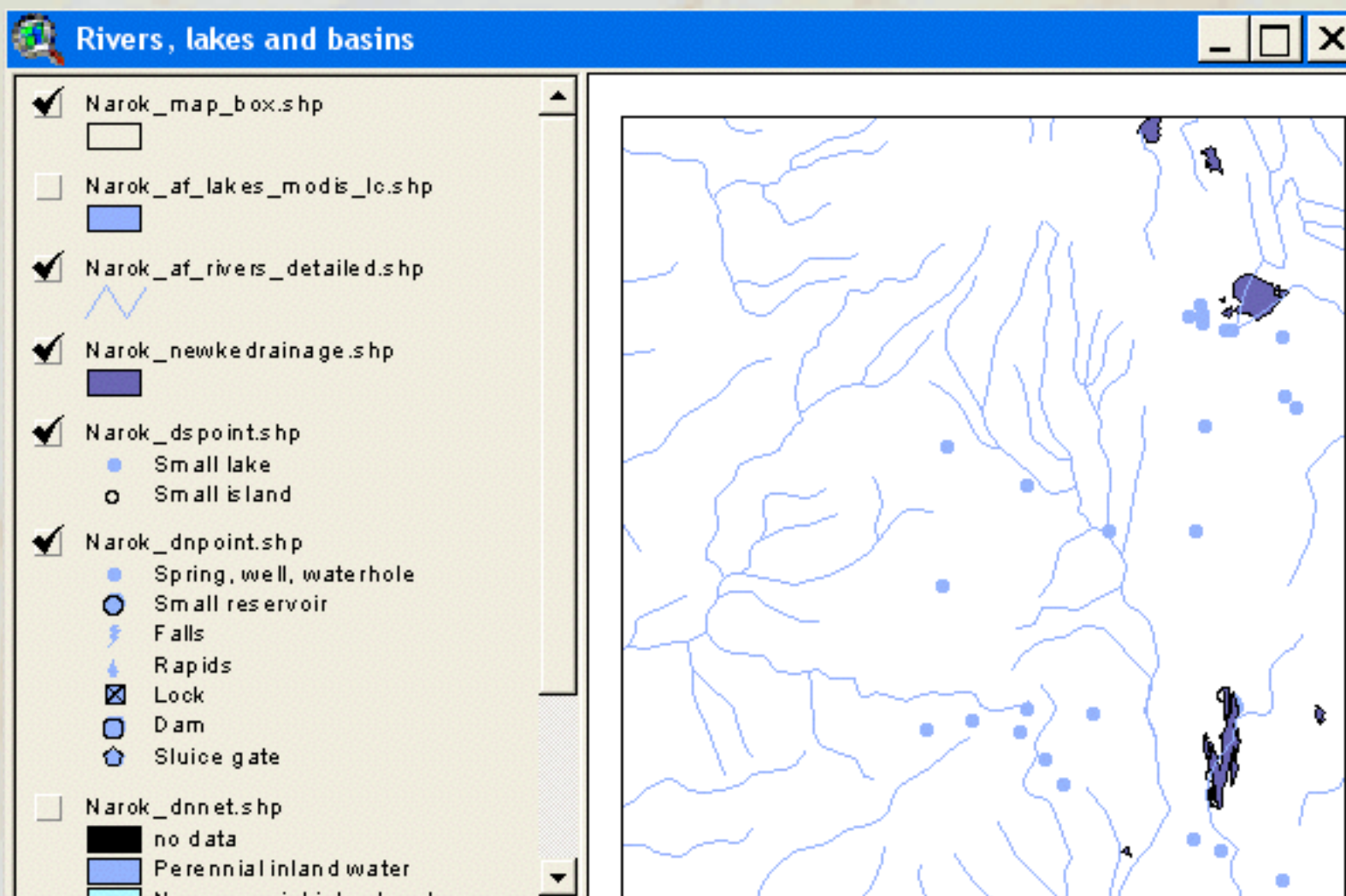
# Example - Thematic mapping for vegetation analysis



# Example - Thematic mapping for vegetation analysis

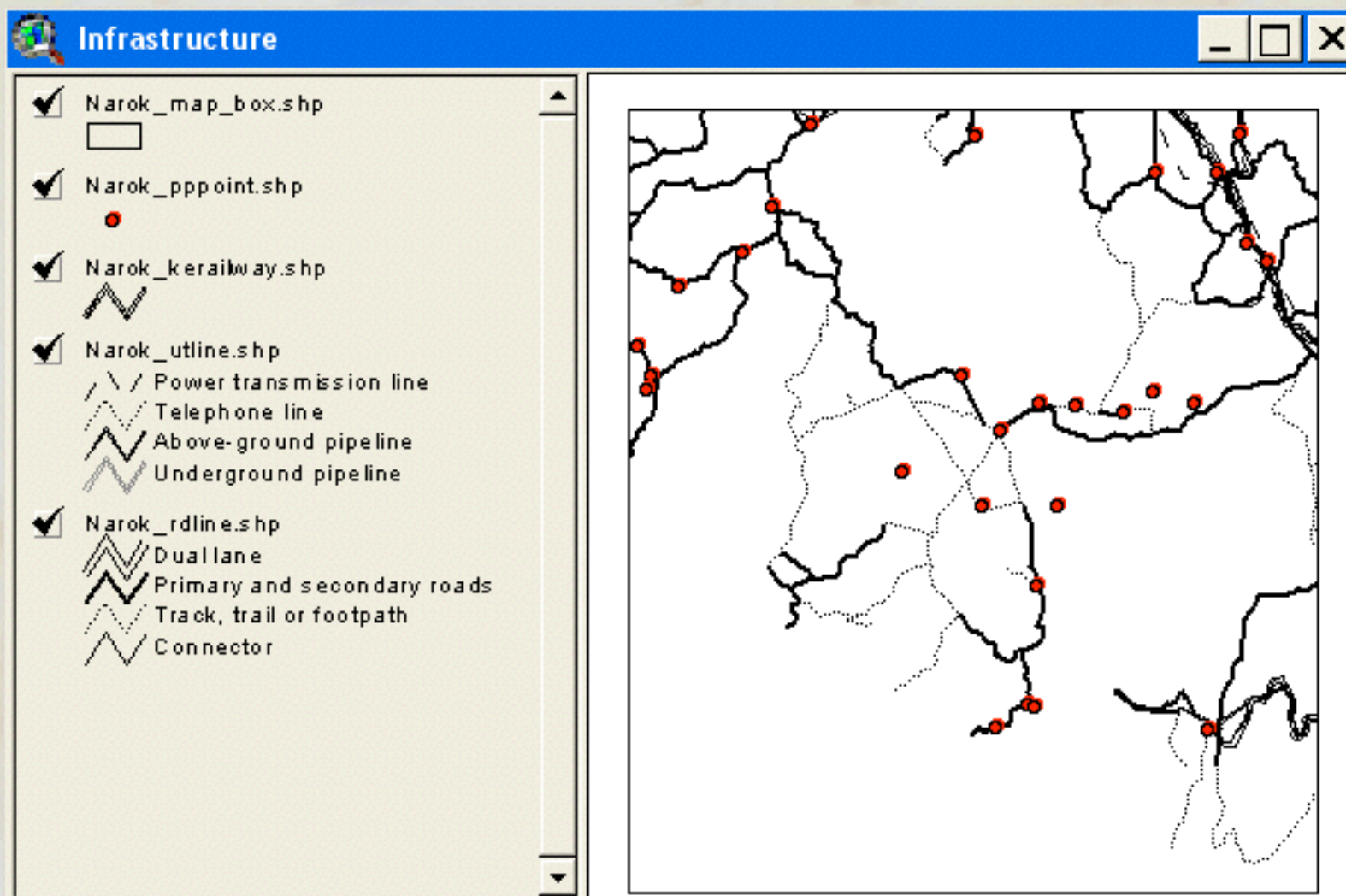


# Example - Thematic mapping for vegetation analysis

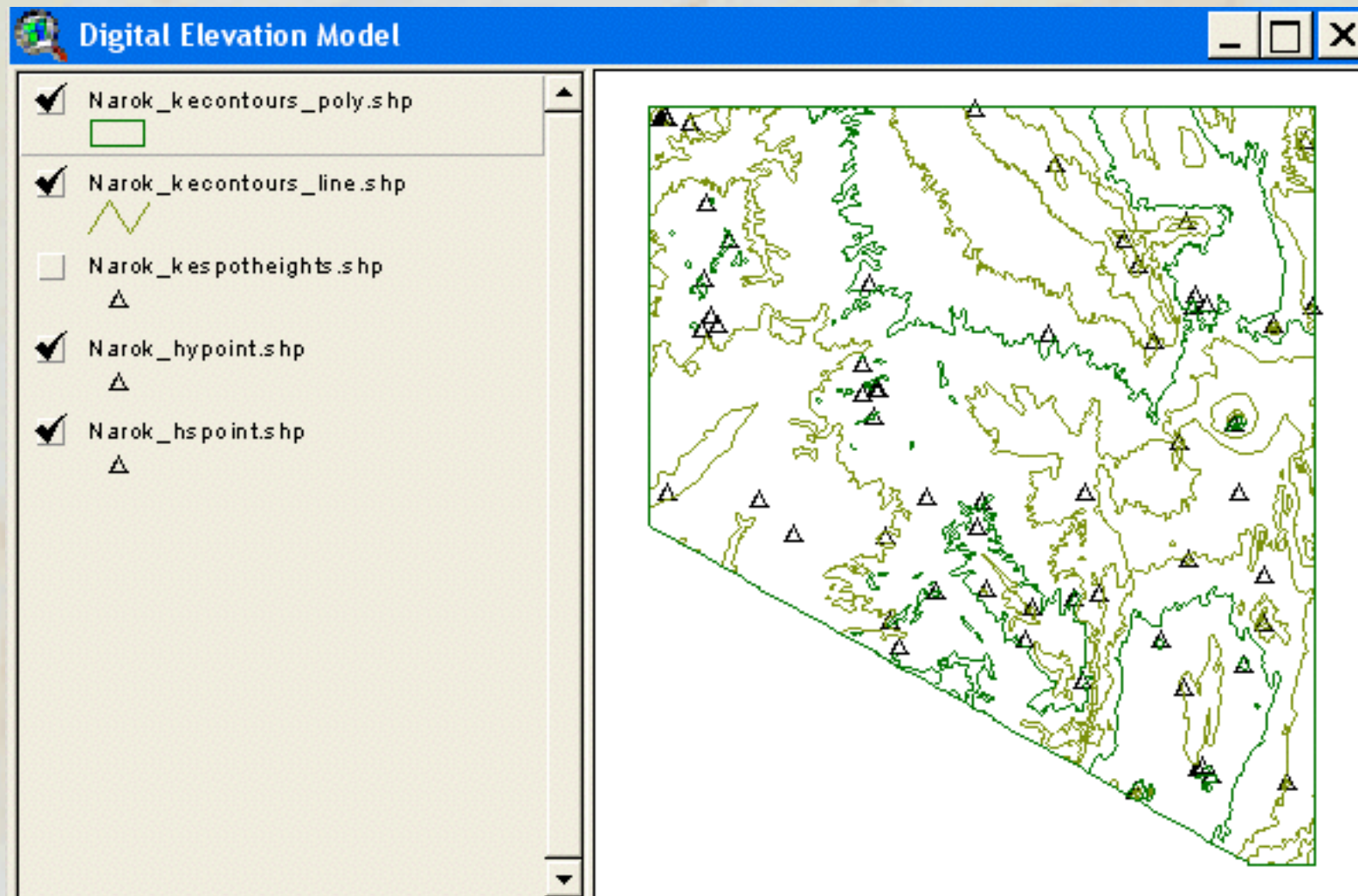




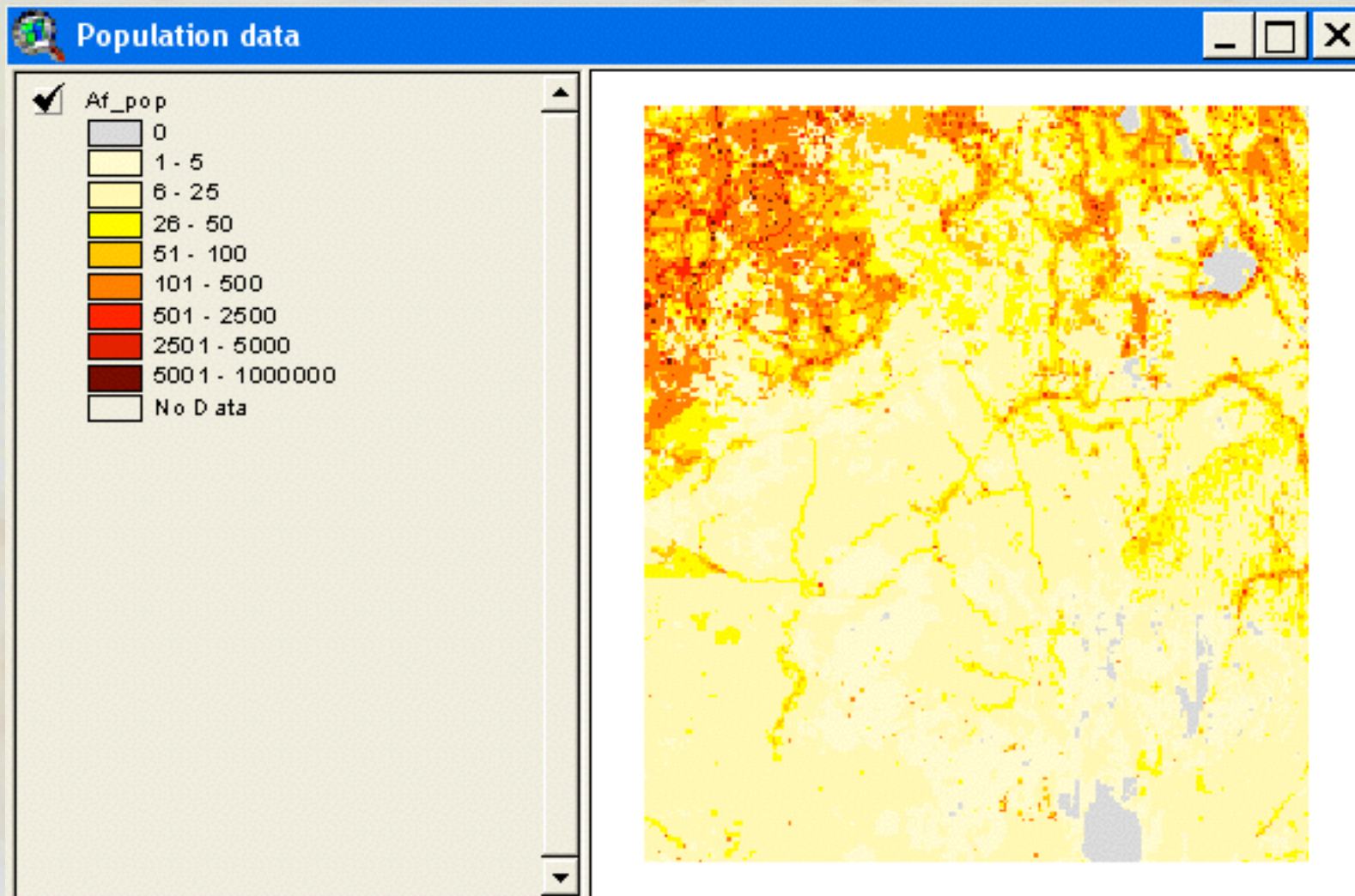
# Example - Thematic mapping for vegetation analysis



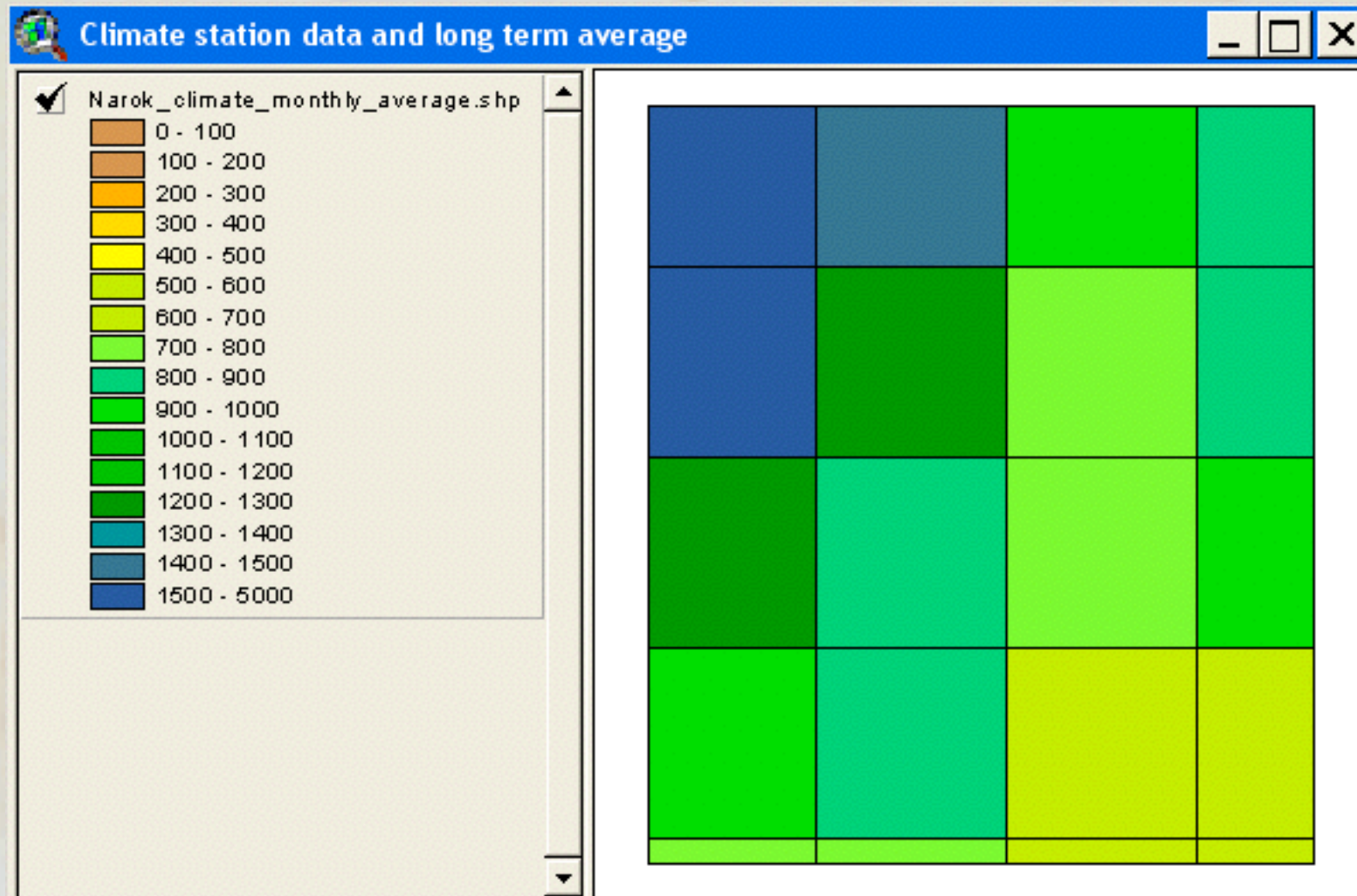
# Example - Thematic mapping for vegetation analysis



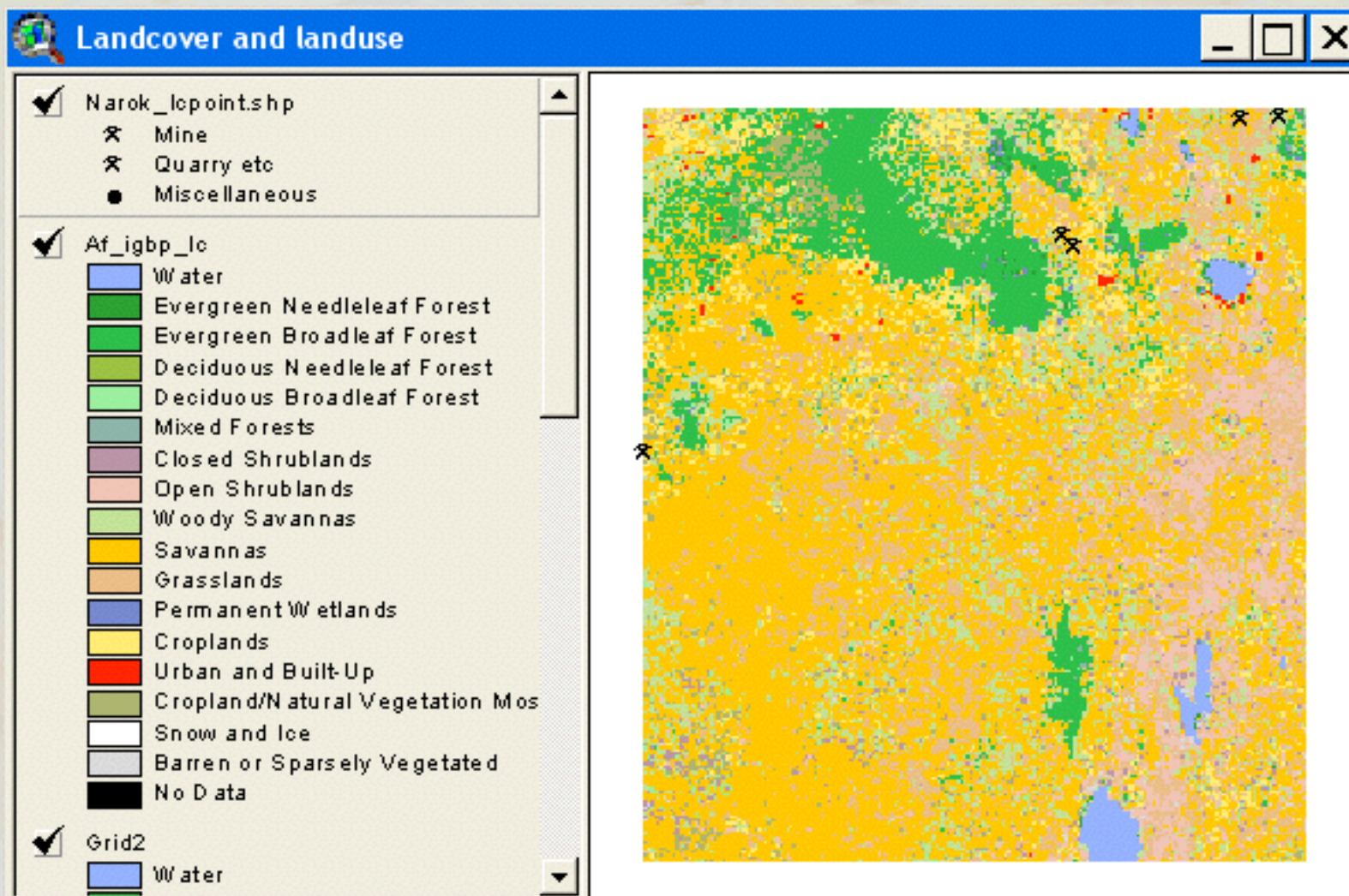
# Example - Thematic mapping for vegetation analysis



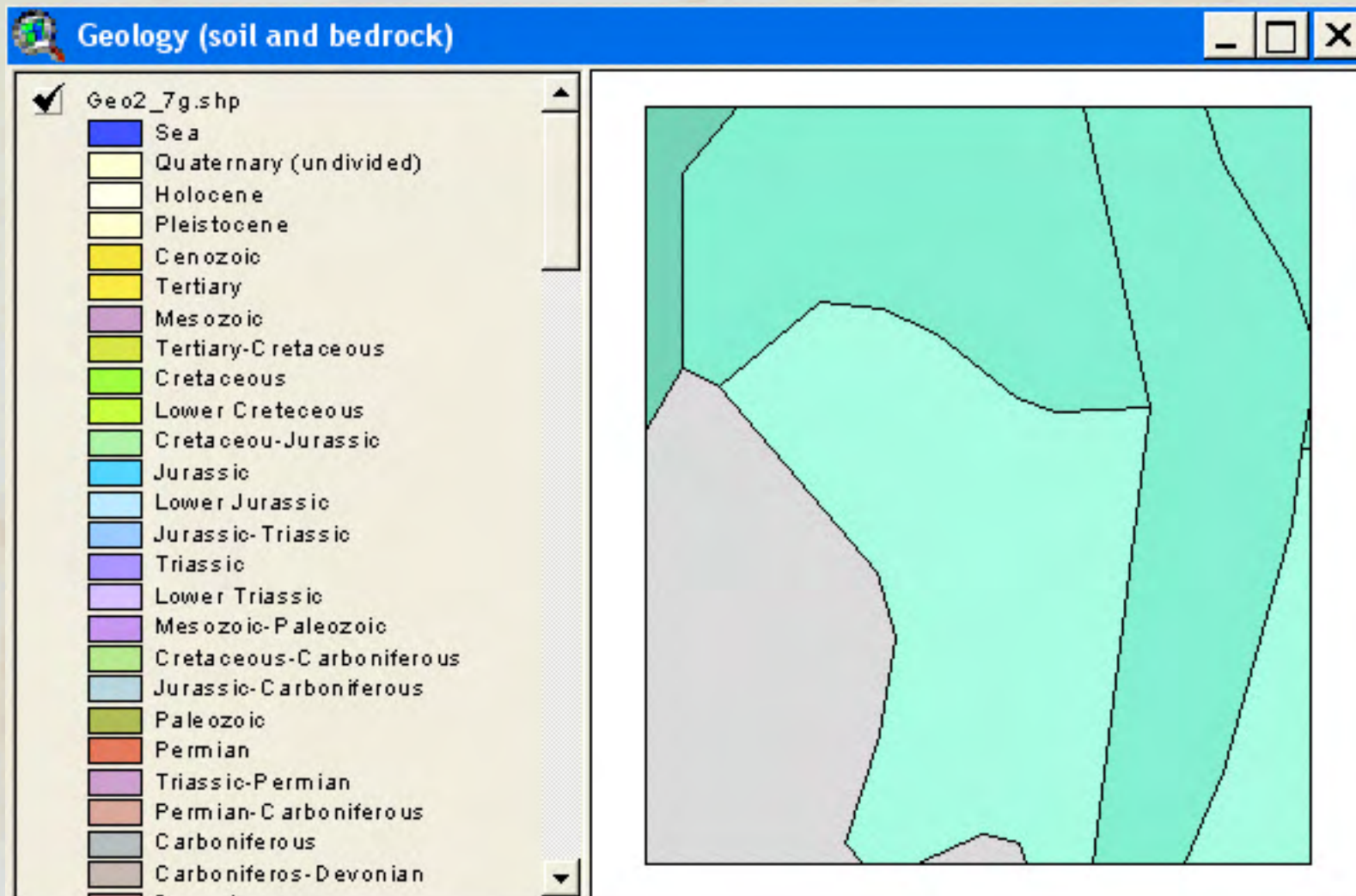
# Example - Thematic mapping for vegetation analysis



# Example - Thematic mapping for vegetation analysis

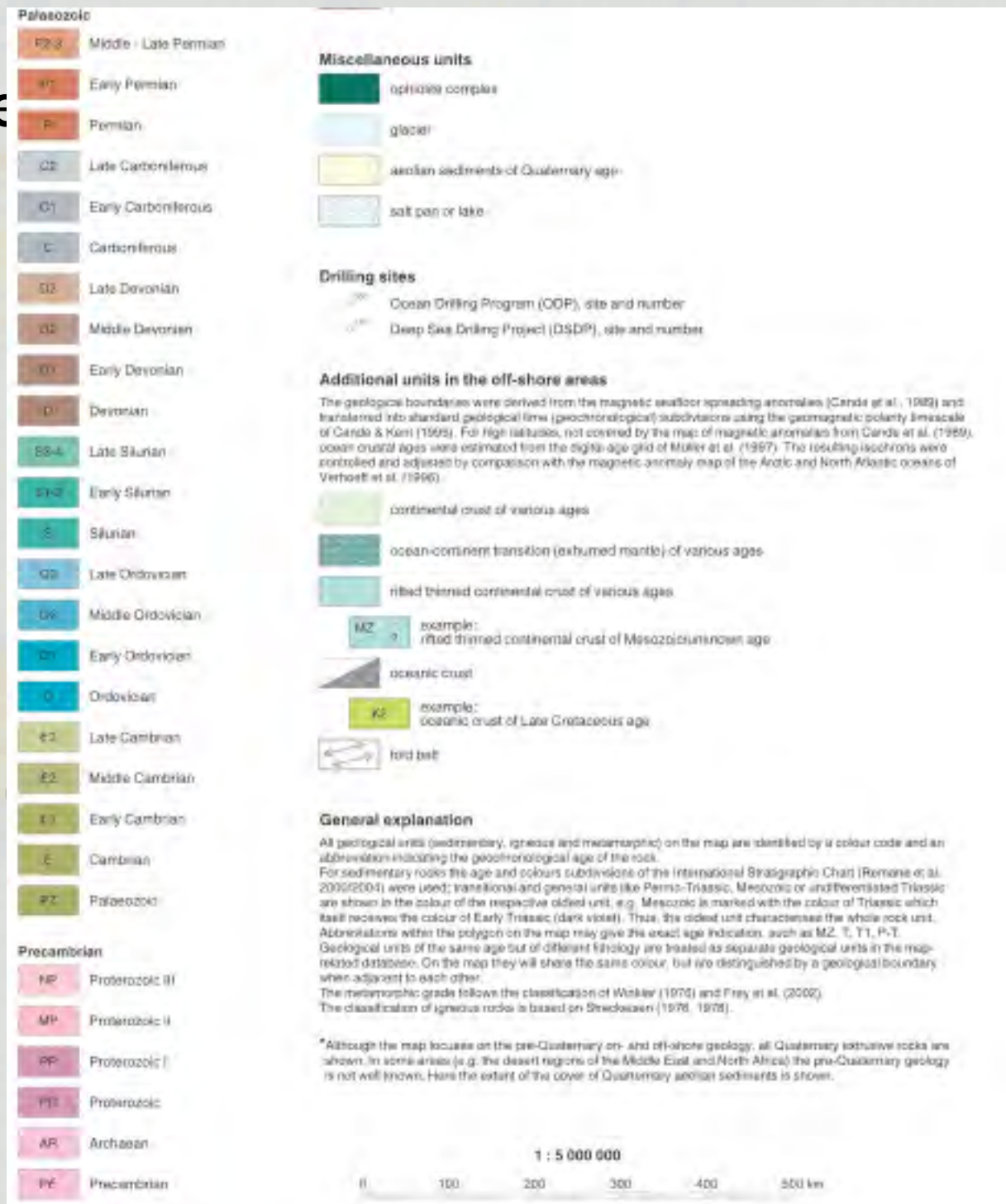


# Example - Thematic mapping for vegetation analysis

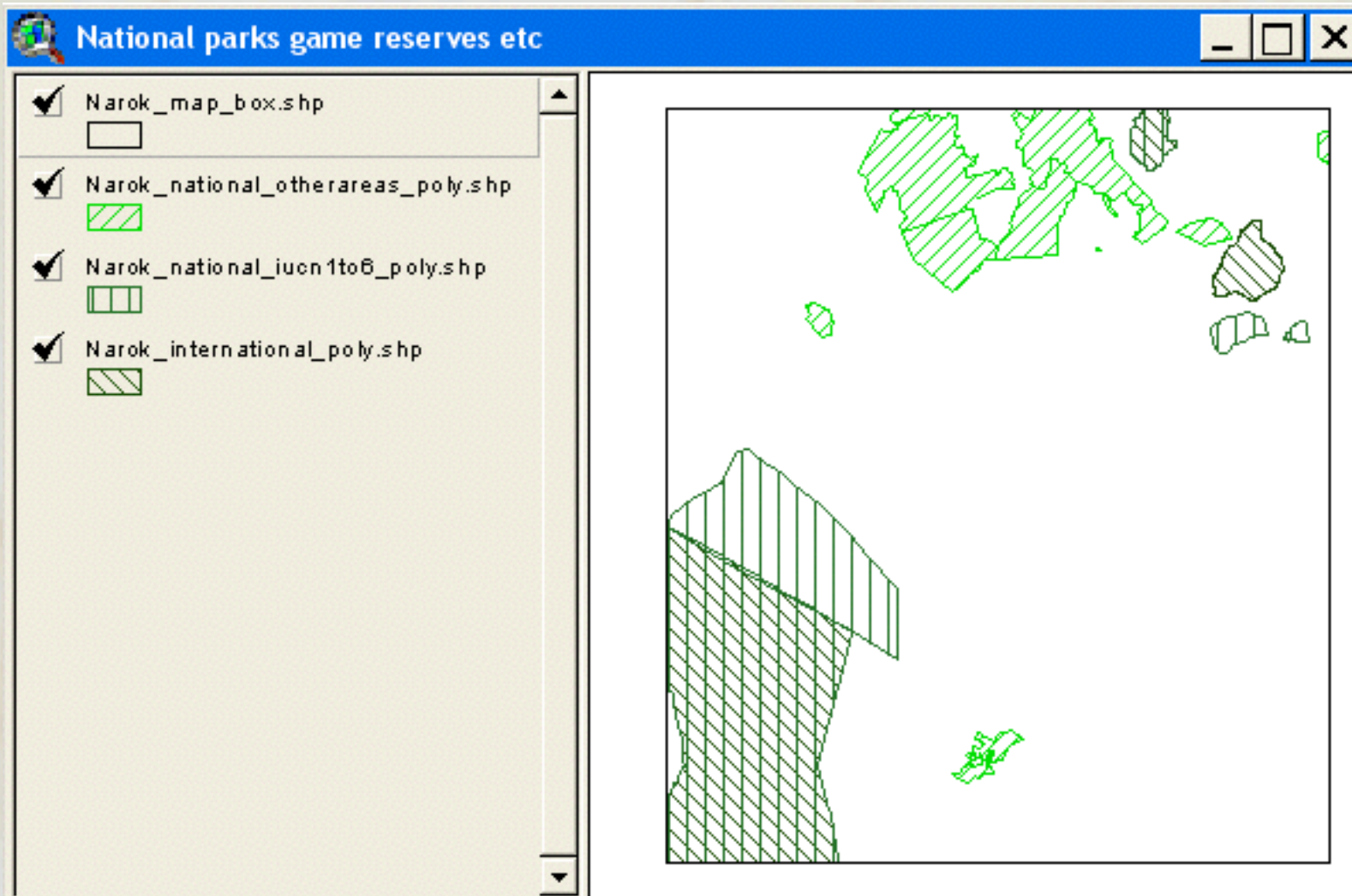


# Example

# analysis

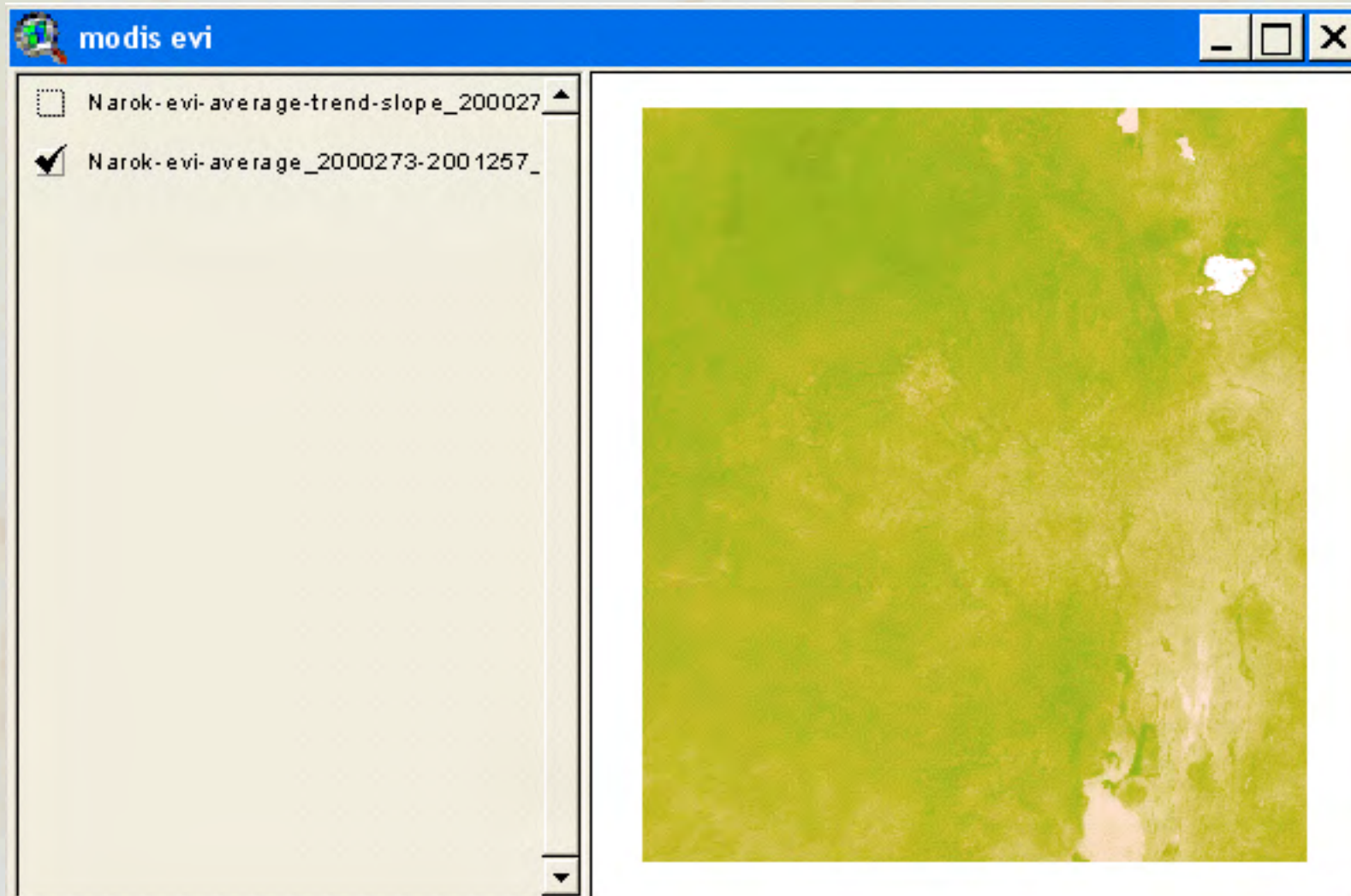


# Example - Thematic mapping for vegetation analysis





# Example - Thematic mapping for vegetation analysis



# Example - Thematic mapping for vegetation analysis

